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AND FREQUENCY CONTROL SOCIETY

# Acoustic Tweezing: Modelling, Implementation and Applications

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IEEE International Ultrasonics Symposium  
Prague, Czech Republic

21 July 2013



# Course Content

The acoustic radiation force

*(Charles Courtney, University of Bath)*

Tweezing with planar resonators

*(Martyn Hill, University of Southampton)*

Dexterous acoustic tweezing

*(Bruce Drinkwater, University of Bristol)*

How to make an acoustic tweezer

*(Sandy Cochran, University of Dundee)*

Applications of acoustics tweezers

*(Martyn Hill, University of Southampton)*



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# **The acoustic radiation force**

(Hand-out to follow)

Dr Charles Courtney  
University of Bath, UK

IEEE International Ultrasonics Symposium  
Prague, Czech Republic  
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# **Tweezing with planar resonators**

(Hand-out to follow)

Professor Martyn Hill  
University of Southampton, UK

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# **Applications of acoustics tweezers**

(Hand-out to follow)

Professor Martyn Hill  
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# **Dexterous Acoustic Tweezing**

Professor Bruce Drinkwater  
University of Bristol, UK

IEEE International Ultrasonics Symposium  
Prague, Czech Republic  
21 July 2013

# Contents

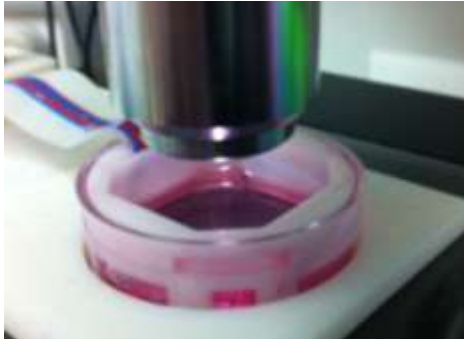
- Introduction to array-based tweezing
- Effect of device boundaries
- Design and modelling of dexterous devices
- High frequency beam-based tweezing
- Current capabilities and future directions



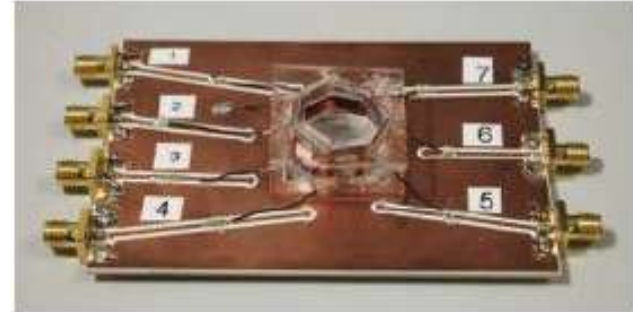


# Examples of array devices

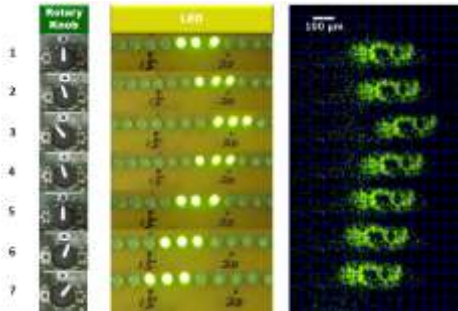
- 4-transducer water-backed<sup>1</sup>



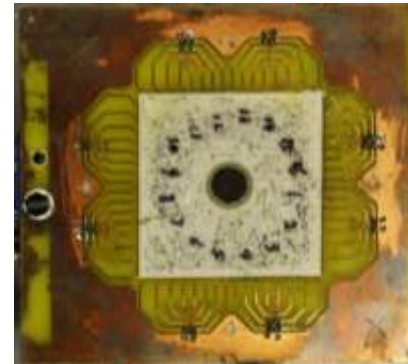
- Heptagon<sup>2</sup>



- Planar array<sup>3</sup>



- Circular array<sup>4</sup>



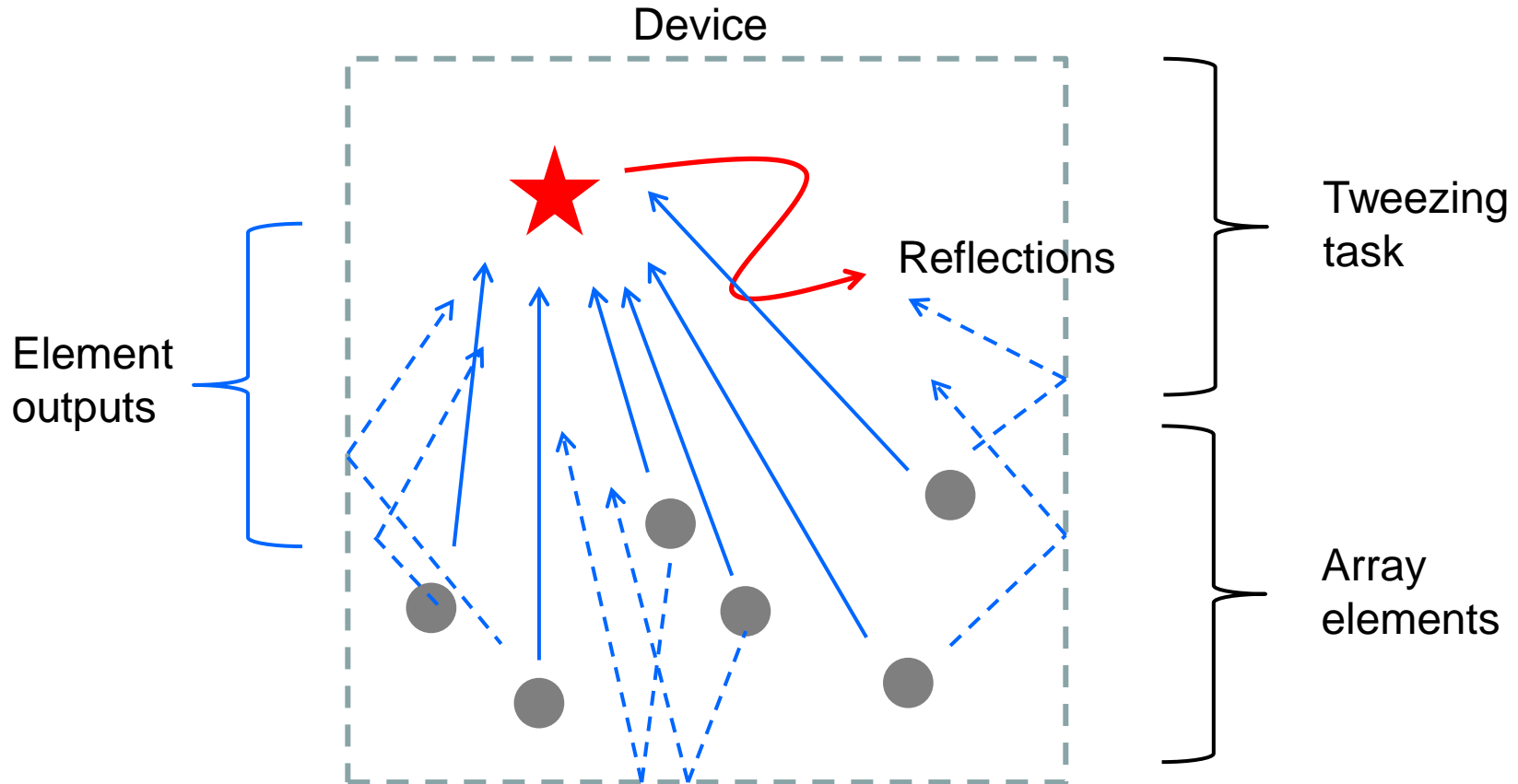
<sup>1</sup>Courtney et al in APL 101 (23), 2012

<sup>2</sup>Bernassau et al in IEEE UFFC 58(10), 2011

<sup>3</sup>Glynne-Jones et al in IEEE UFFC 59(6), 2012

<sup>4</sup>Courtney et al in APL 102 (12), 2013

# 🔥 Array-based manipulation



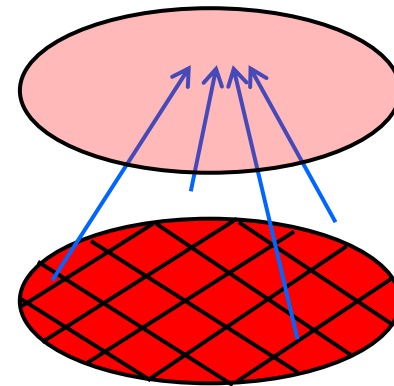
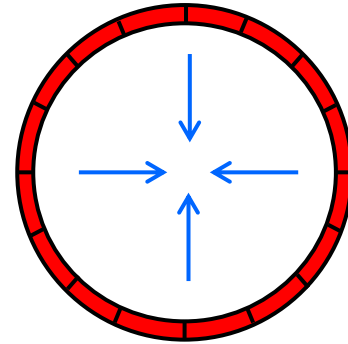
# Questions

- How to arrange the array elements?
- What acoustic field is needed to complete the tweezing task?
- How can this required acoustic field be created?
- What is the influence of the device boundaries?



# 🔥 Current devices

- Surround the region with elements for in-plane tweezing
- Use a plane of elements to create a beam for out-of-plane tweezing



Device boundary

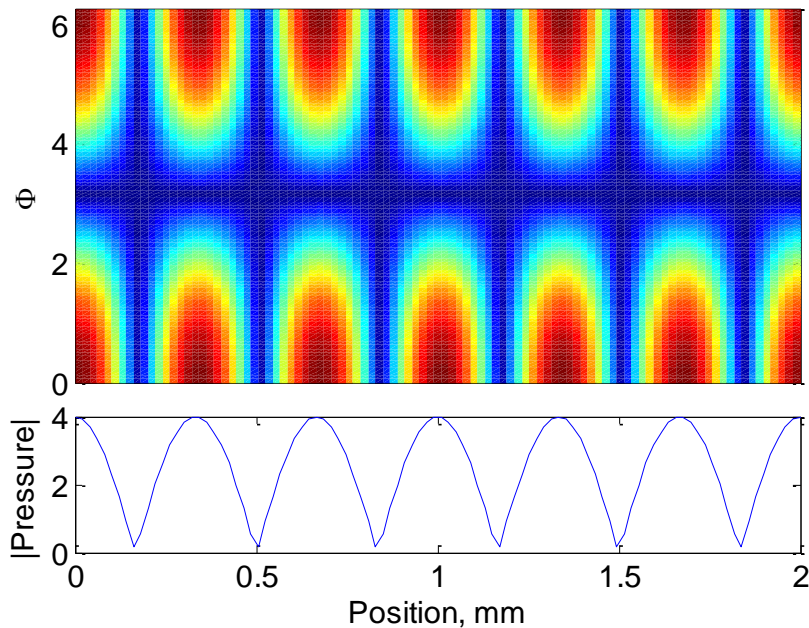
These concepts could be merged for 3D manipulation

# Effect of boundaries

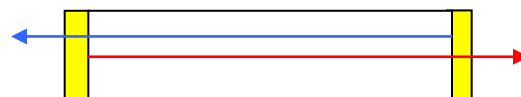
## Reflective boundaries



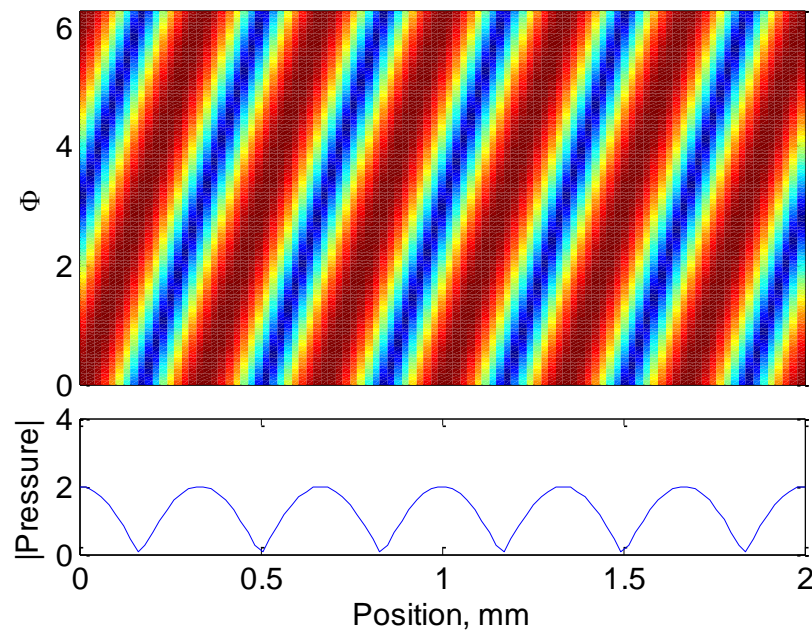
$$u(x) = 2A[\cos(kx) + e^{i\phi/2}\cos(kx)]$$



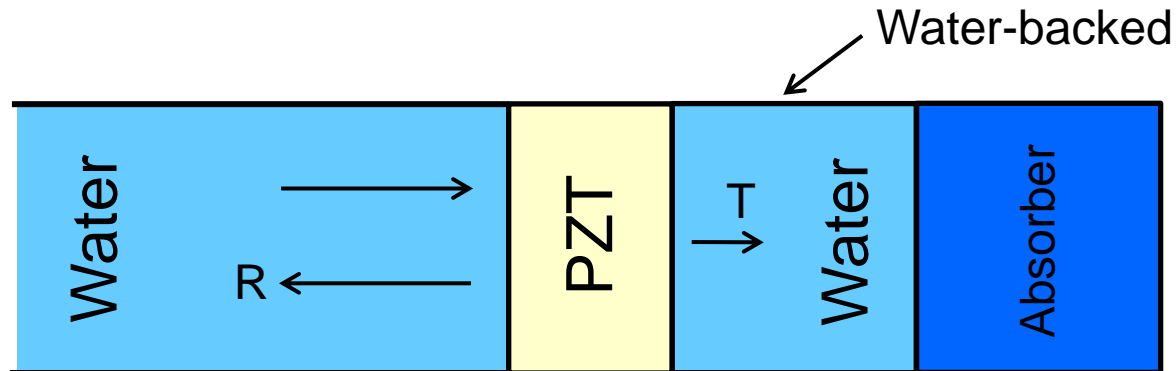
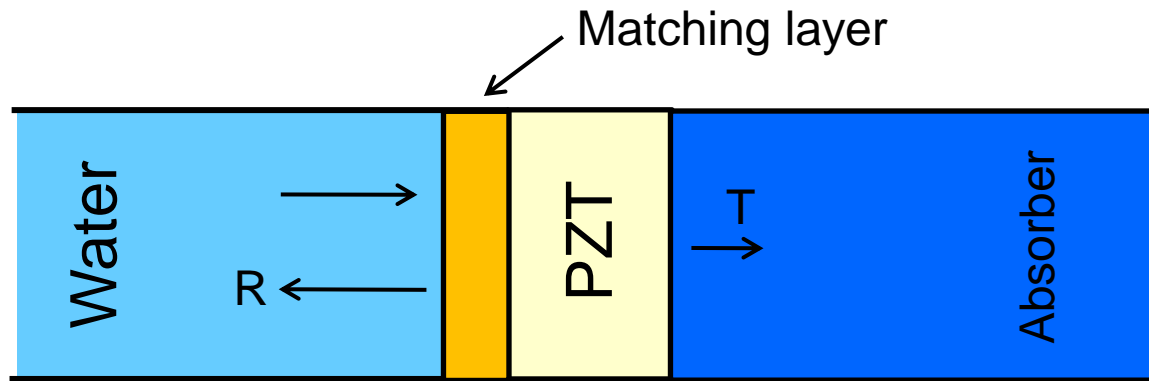
## Transparent boundaries



$$u(x) = A[e^{ikx} + e^{-i(kx-\phi)}]$$

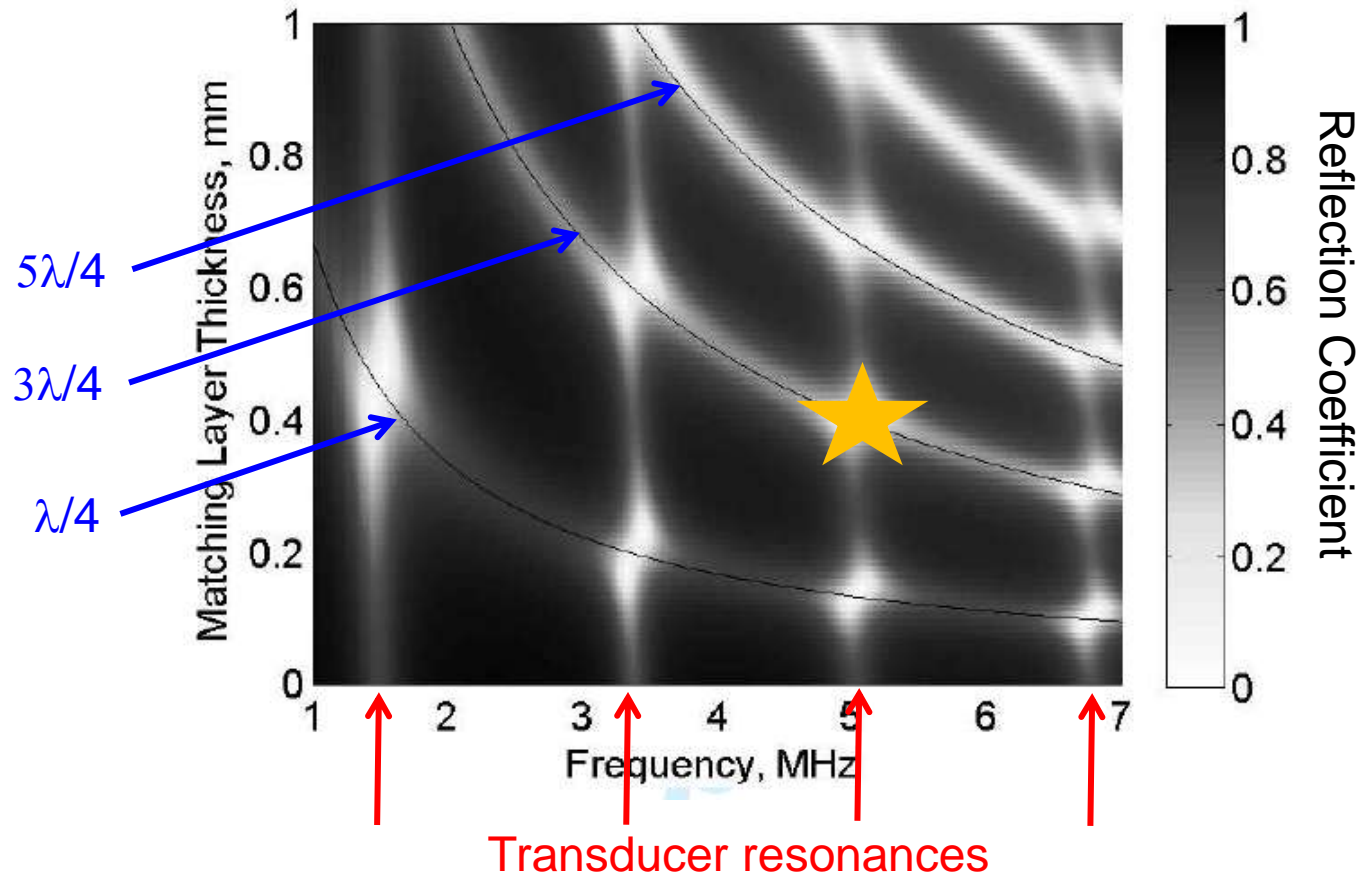


# Transparent boundaries

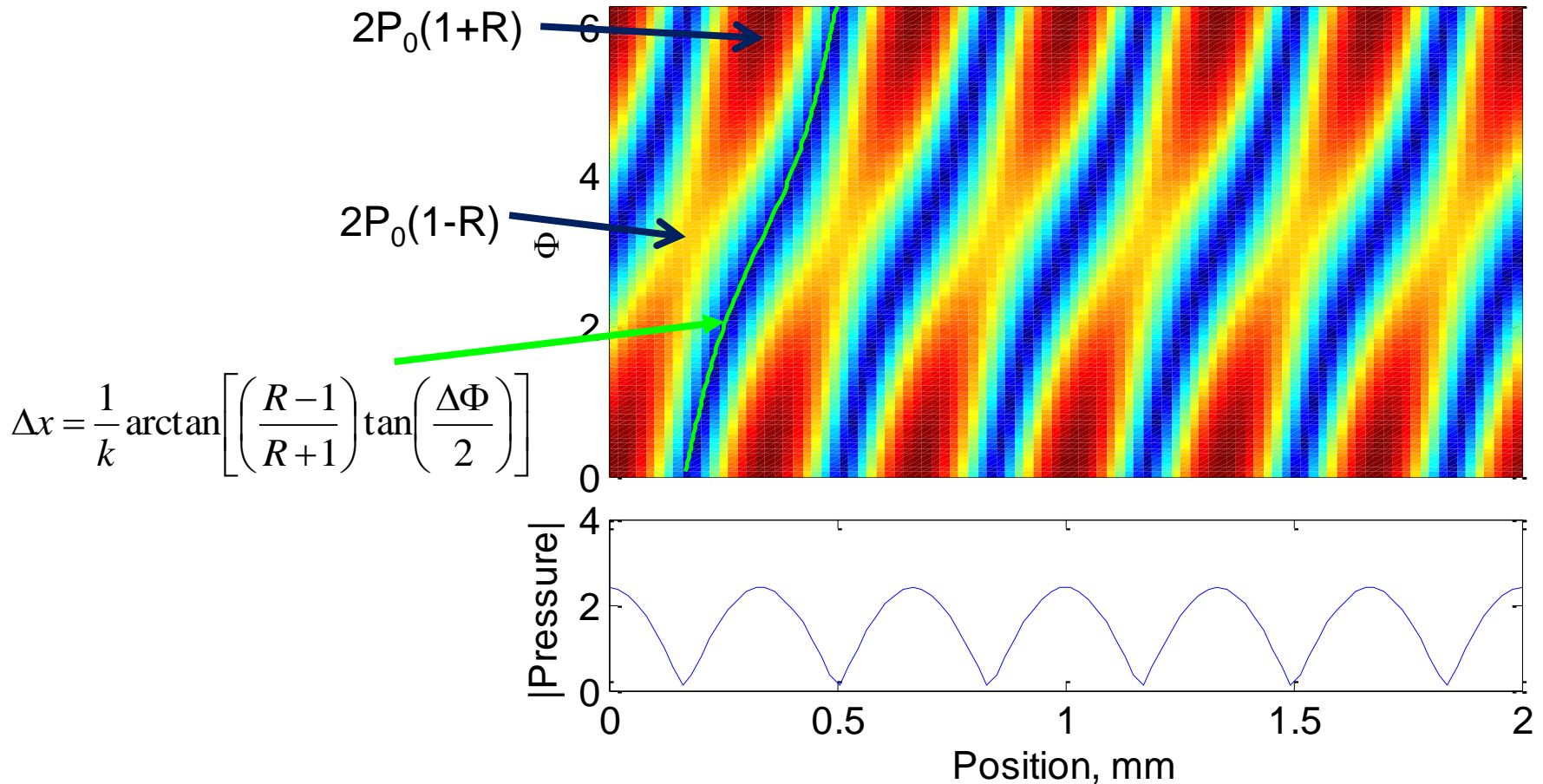


# 🔥 Transparent boundaries

- Matching layer design

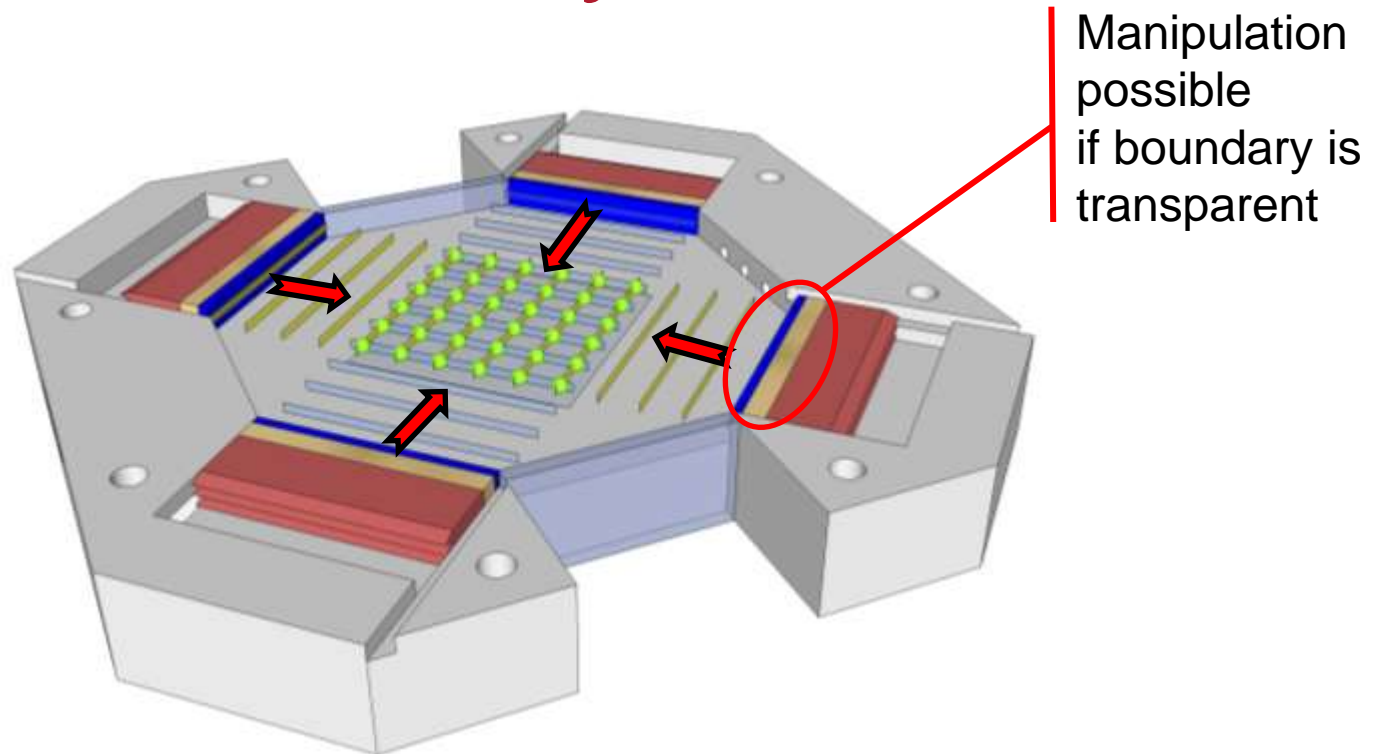


# Effect of partial reflection



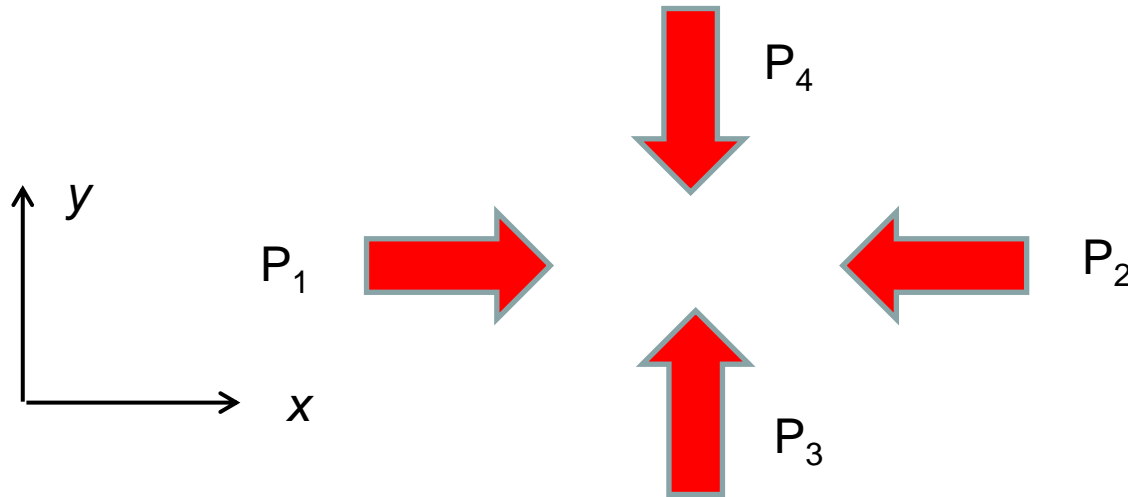


# 🔥 4-element array



- Rectangular grid pattern formed
- Grid can be translated in the plane of the device
- Applications in biology and materials

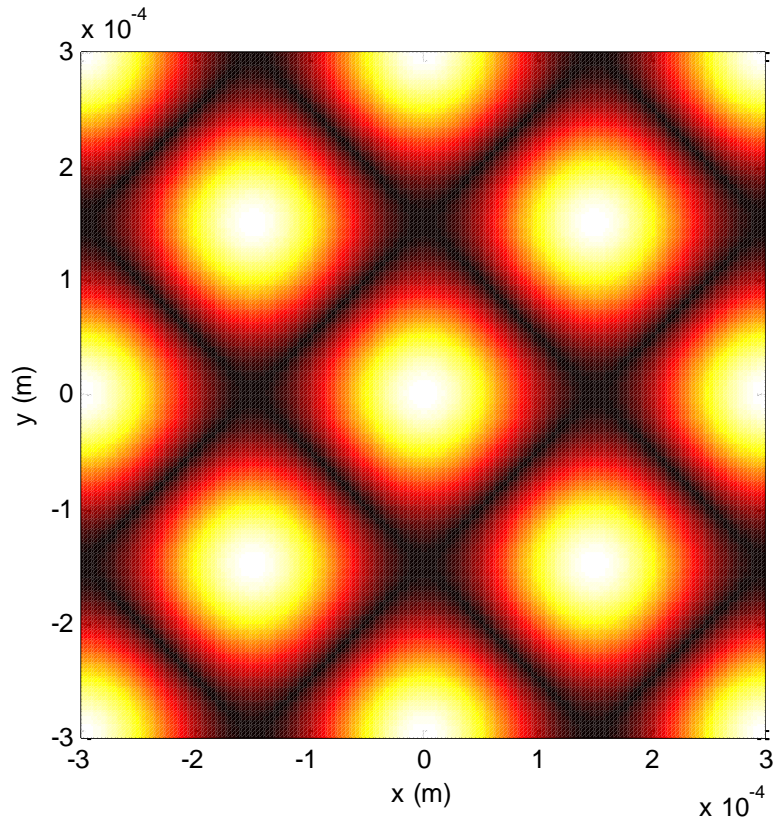
# 🔥 Simulating the device



$$P_1(x, y) = P_0 \exp[i(kx + \varphi_1)]$$
$$P_2(x, y) = P_0 \exp[i(-kx + \varphi_2)]$$
$$P_3(x, y) = P_0 \exp[i(ky + \varphi_3)]$$
$$P_4(x, y) = P_0 \exp[i(-ky + \varphi_4)]$$

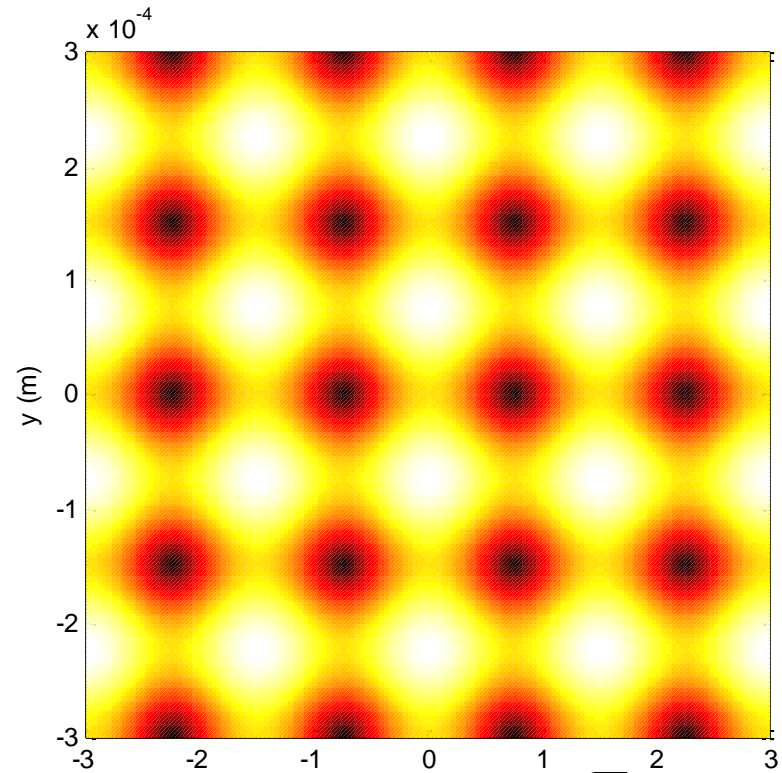
4 plane  
waves, no  
reflections

# Acoustic Pressure



$$\phi_y = \phi_x$$

Where,  $\phi_x = \frac{\varphi_1 + \varphi_2}{2}$ , and  $\phi_y = \frac{\varphi_3 + \varphi_4}{2}$



$$\phi_y = \phi_x + \frac{\pi}{2}$$

# 🔥 Acoustic radiation force

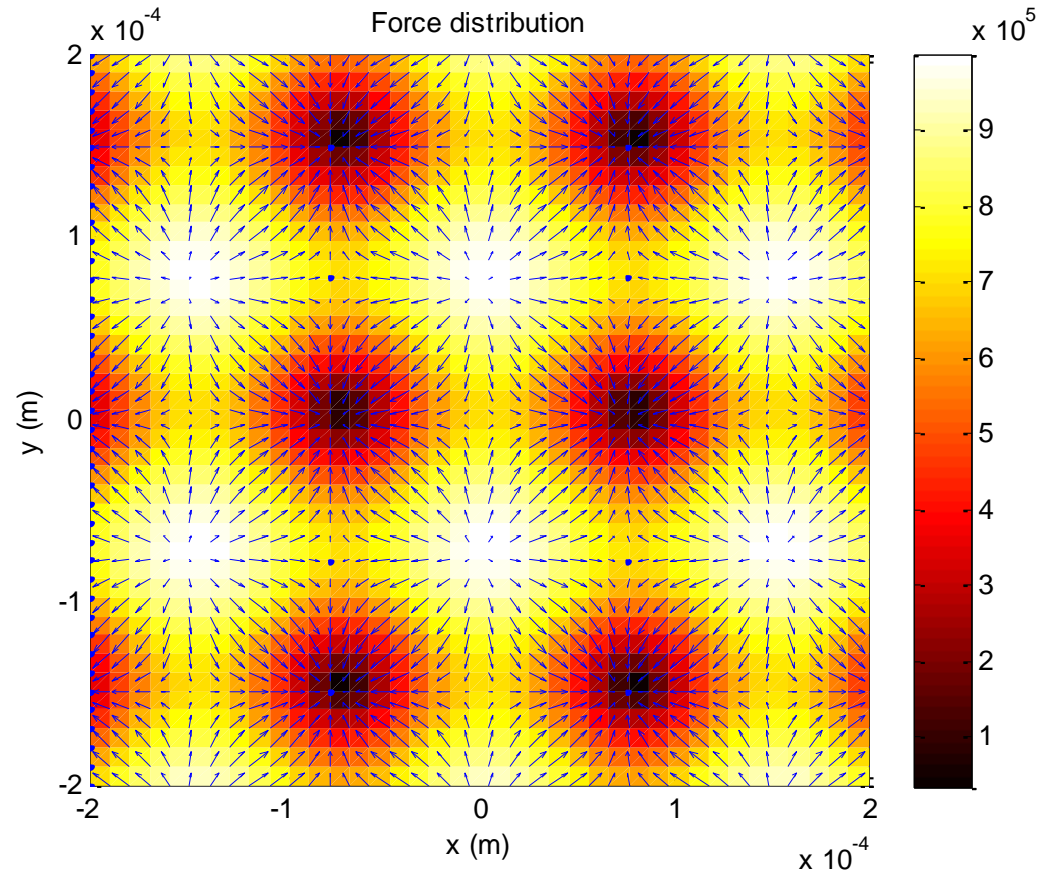
- Using Gor'kov  $U = 2\pi a^3 \rho \left\{ \frac{\overline{P^2}}{3\rho^2 c^2} f_1 - \frac{\overline{v^2}}{2} f_2 \right\}$

- $f_1 = 1 - \frac{K}{K_0}$

- $f_2 = 2 \frac{\rho_0 - \rho}{2\rho_0 + \rho}$

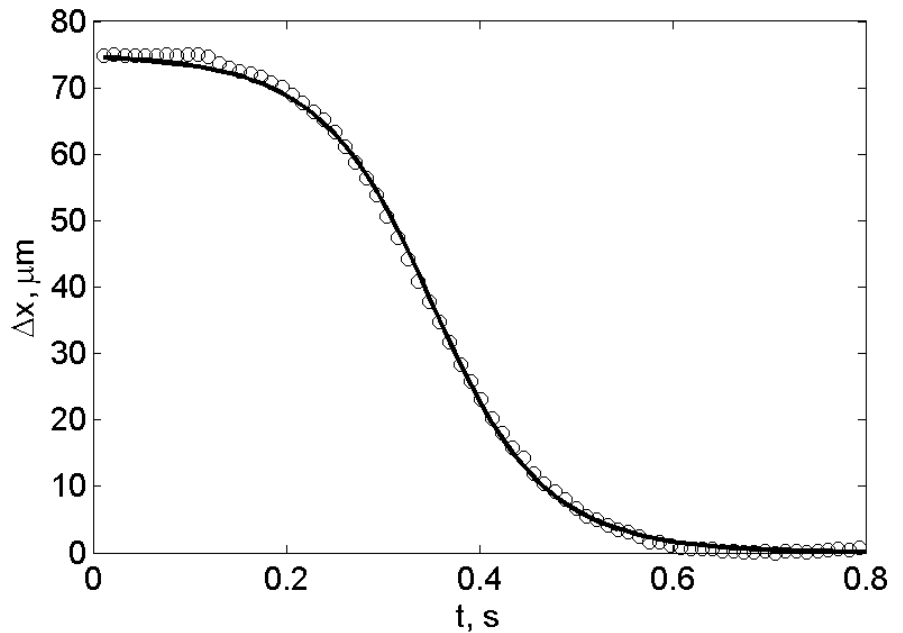
And then

- $F = -\nabla U$



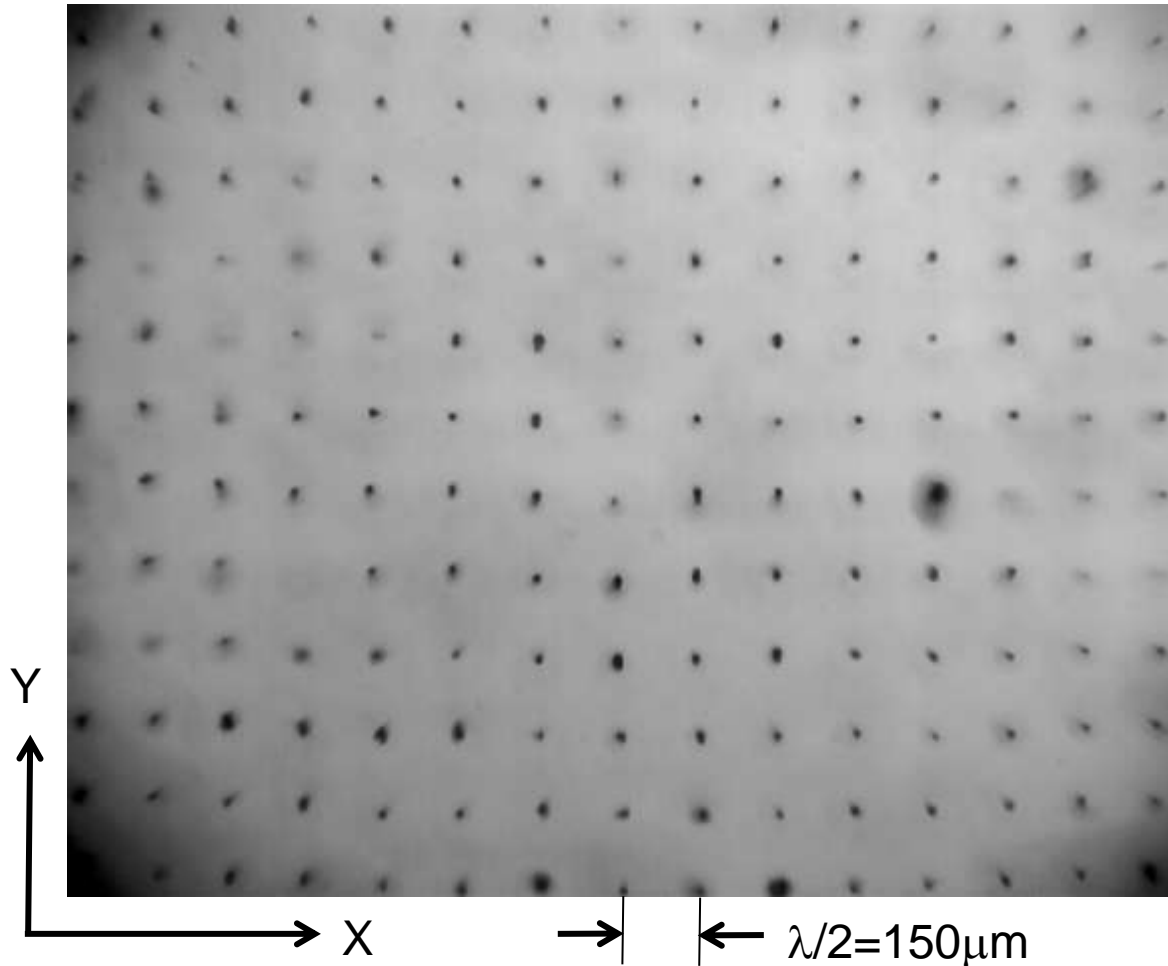
# 🔥 Force Measurement

- Locate single particle in trap.
- Shift acoustic field by  $\lambda / 2$ .
- Track motion with 200 fps camera.
- Fit solution for particle in sinusoidal potential well in presence of Stoke's drag



$$F_0 = 30 \text{ pN}$$

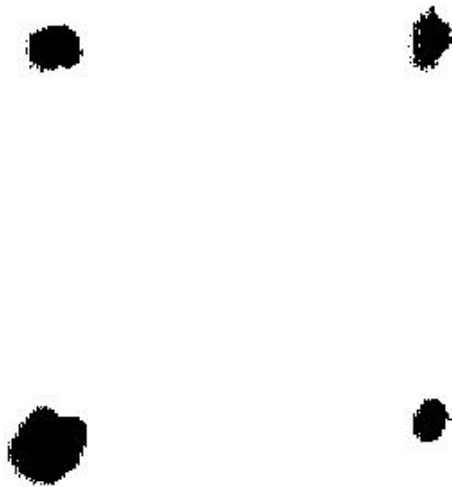
# 🌟 10,000 trapping points



- Uniform grid of equal traps
- Translatable in X and Y

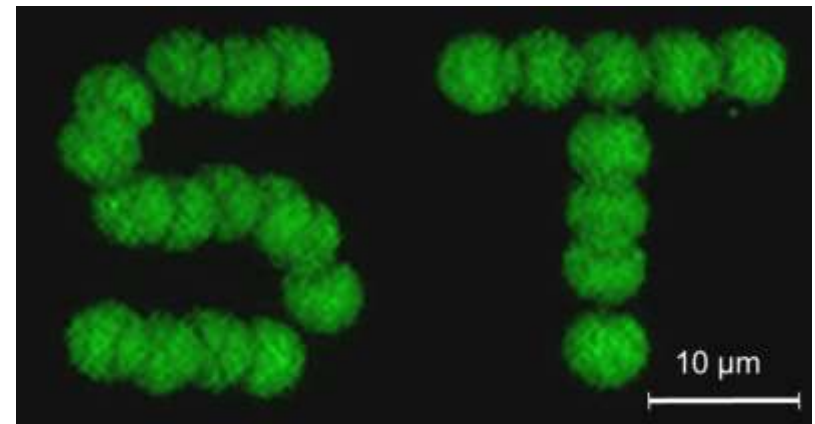
# 🔥 Translation of the acoustic field

Video



Four 10  $\mu\text{m}$  particles

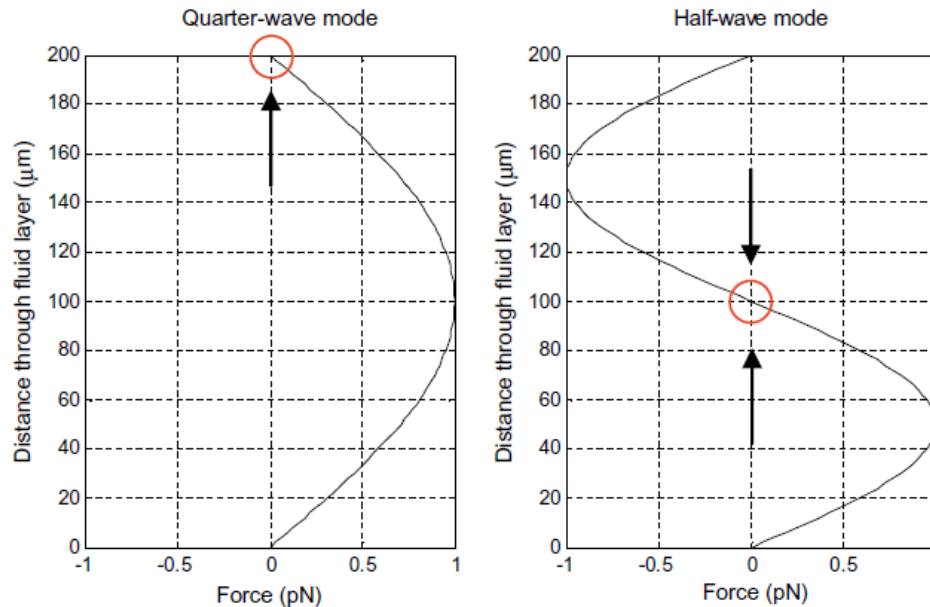
Composite photo



Composite image of a single 6  $\mu\text{m}$  fluorescent particle maneuvered to shape the letters 'ST'

# Alternative concepts

- Mode switching

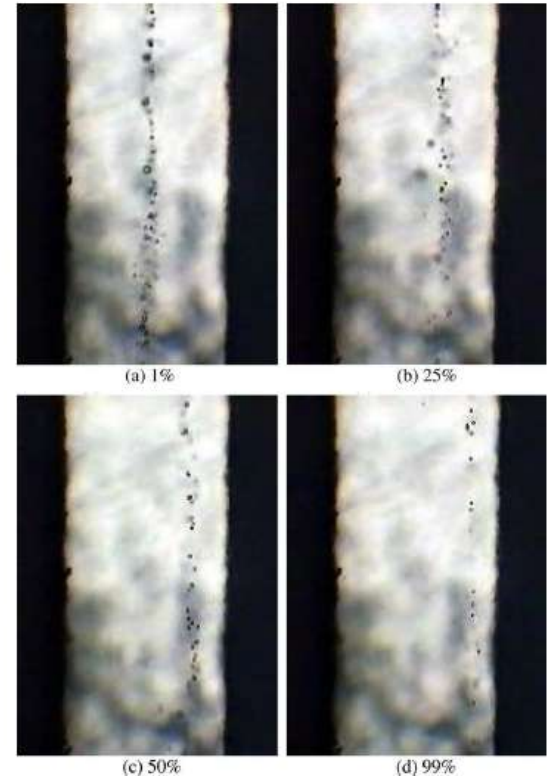
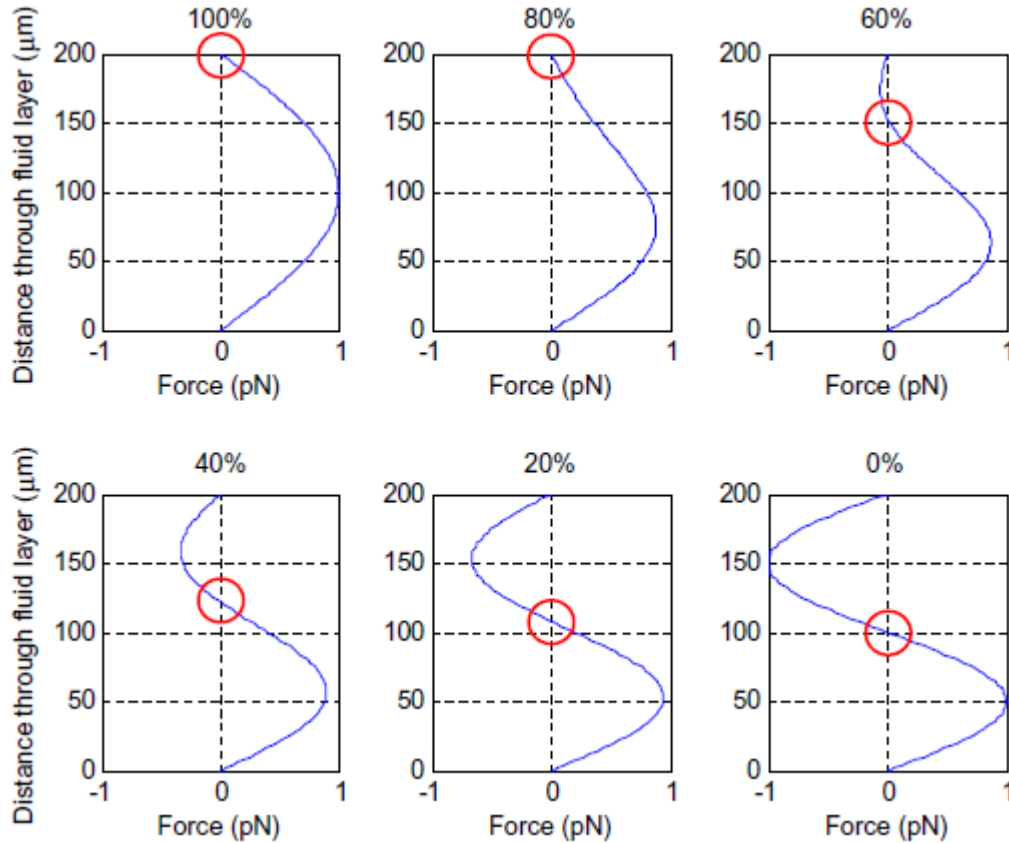


- $F_{Total} = qF_Q + (1 - q)F_H$

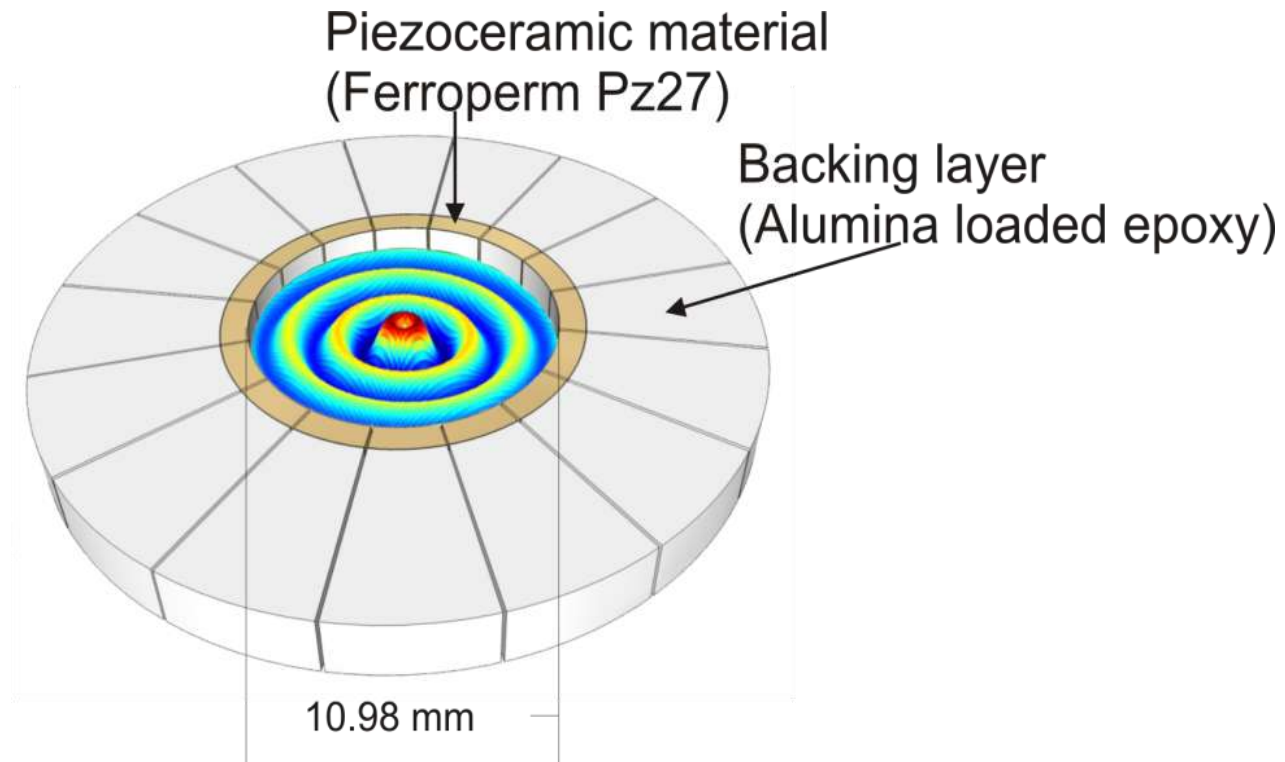
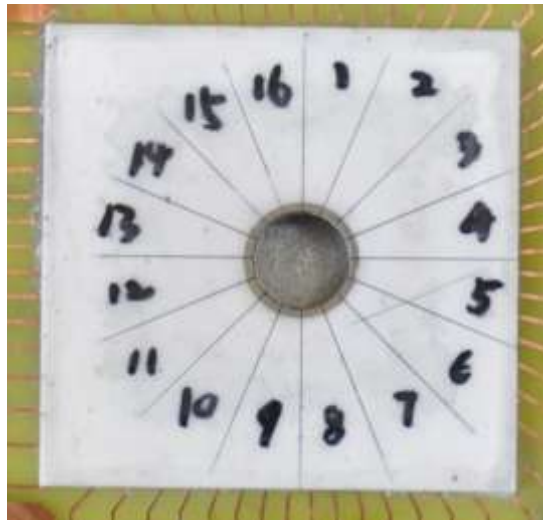


# Mode switching

Varying the fraction of the quarter wavelength mode

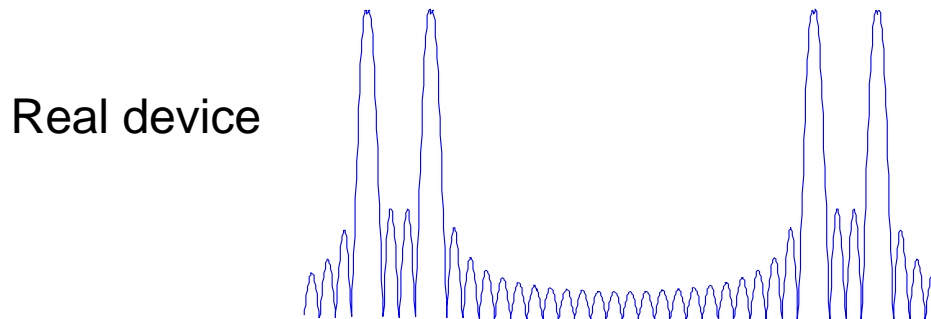
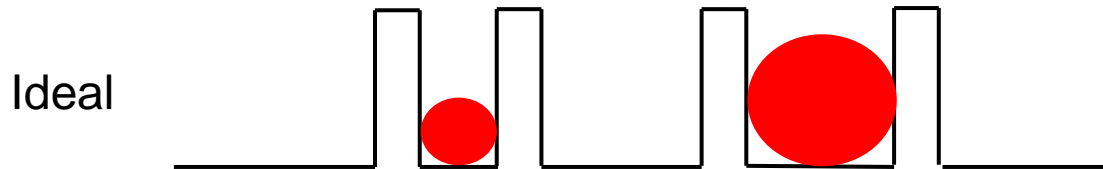


# 🔥 Circular Array Device



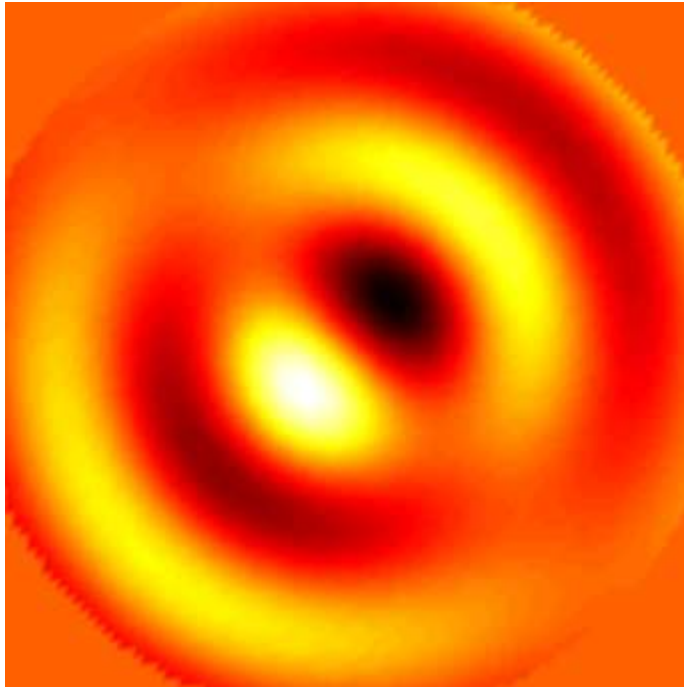
# 🔥 Ideal acoustic pressure field?

- Arbitrary trap locations
- Arbitrary trap numbers
- Sharp spatial gradients
- Minimal interference between traps

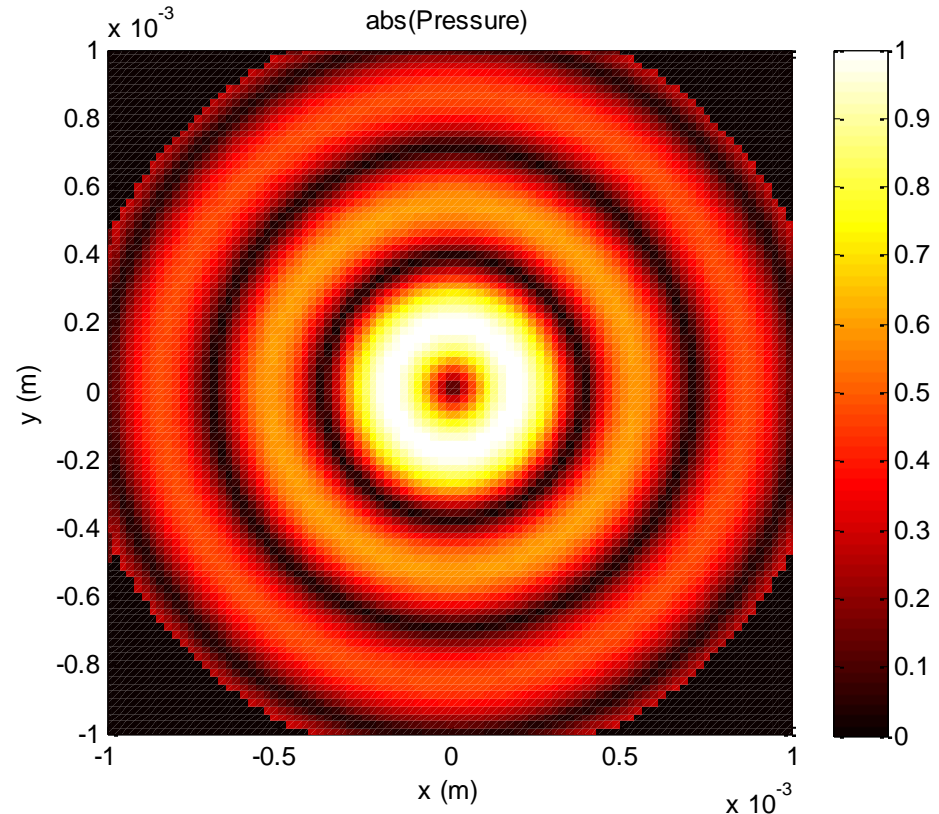


# 🔥 Helical\* beam creates local minima

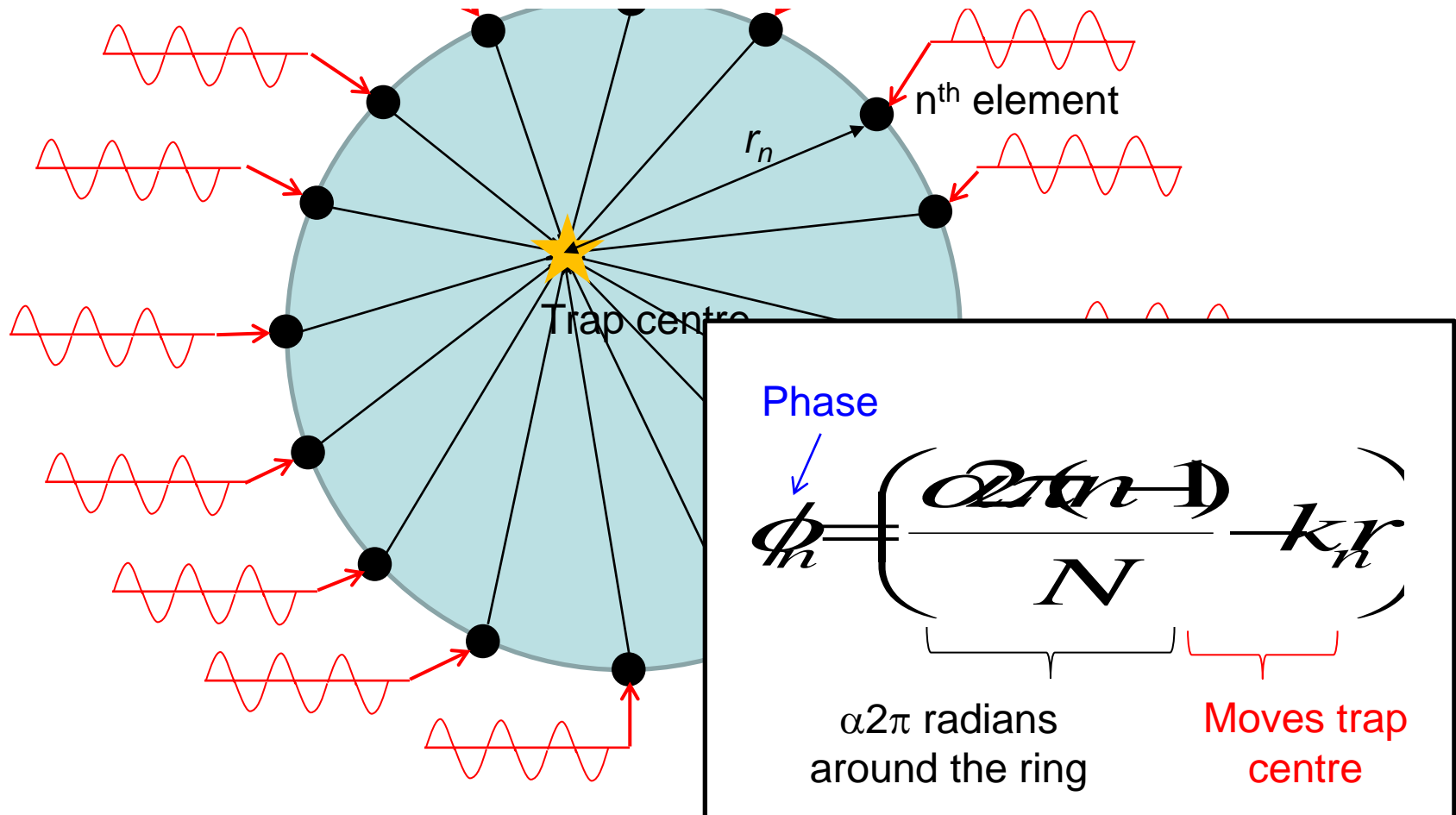
Instantaneous pressure ( $\alpha=1$ )



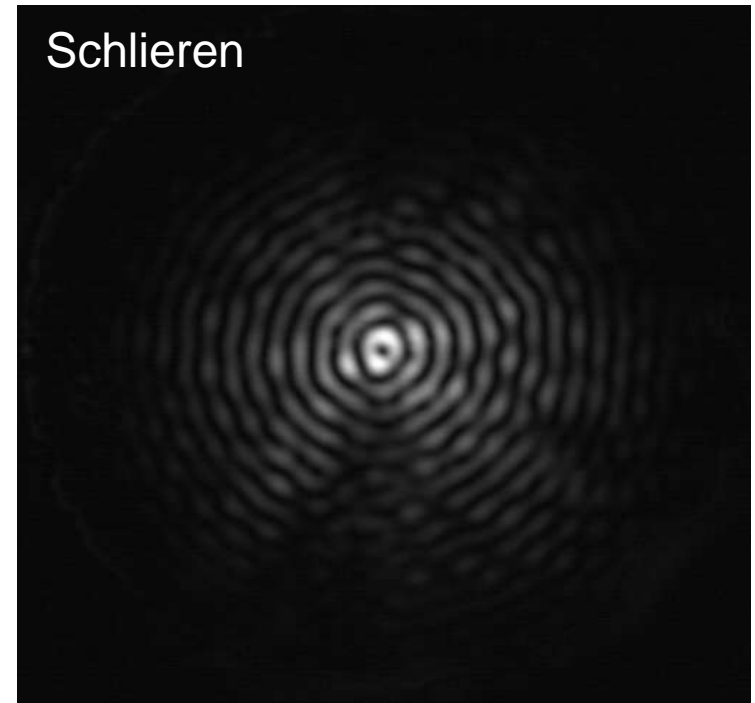
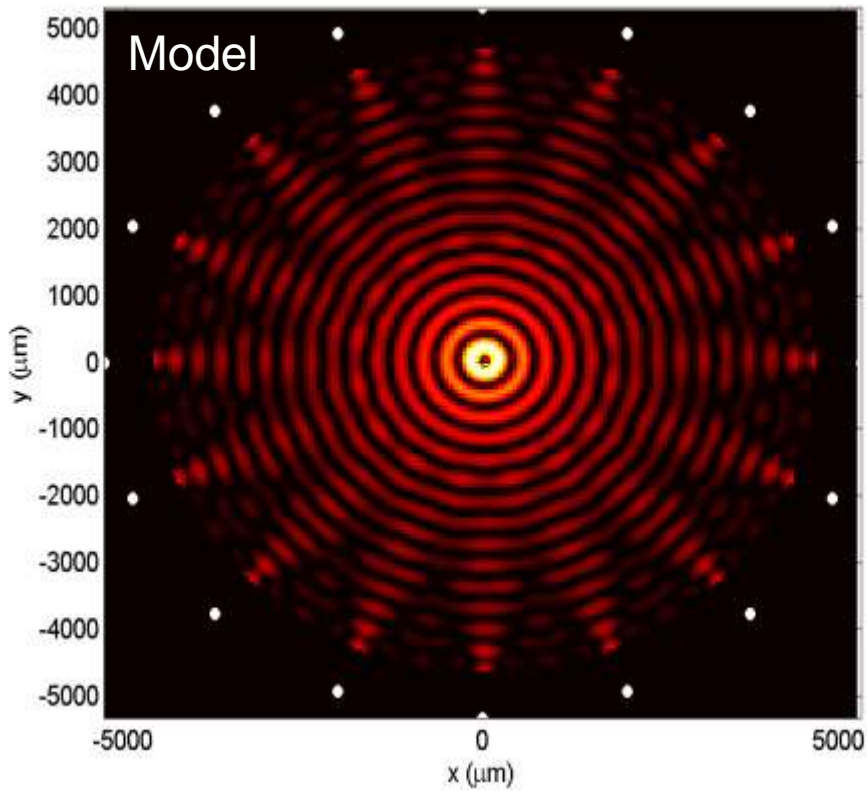
$\alpha$ =topological charge



# 🌟 How to generate a Helical beam

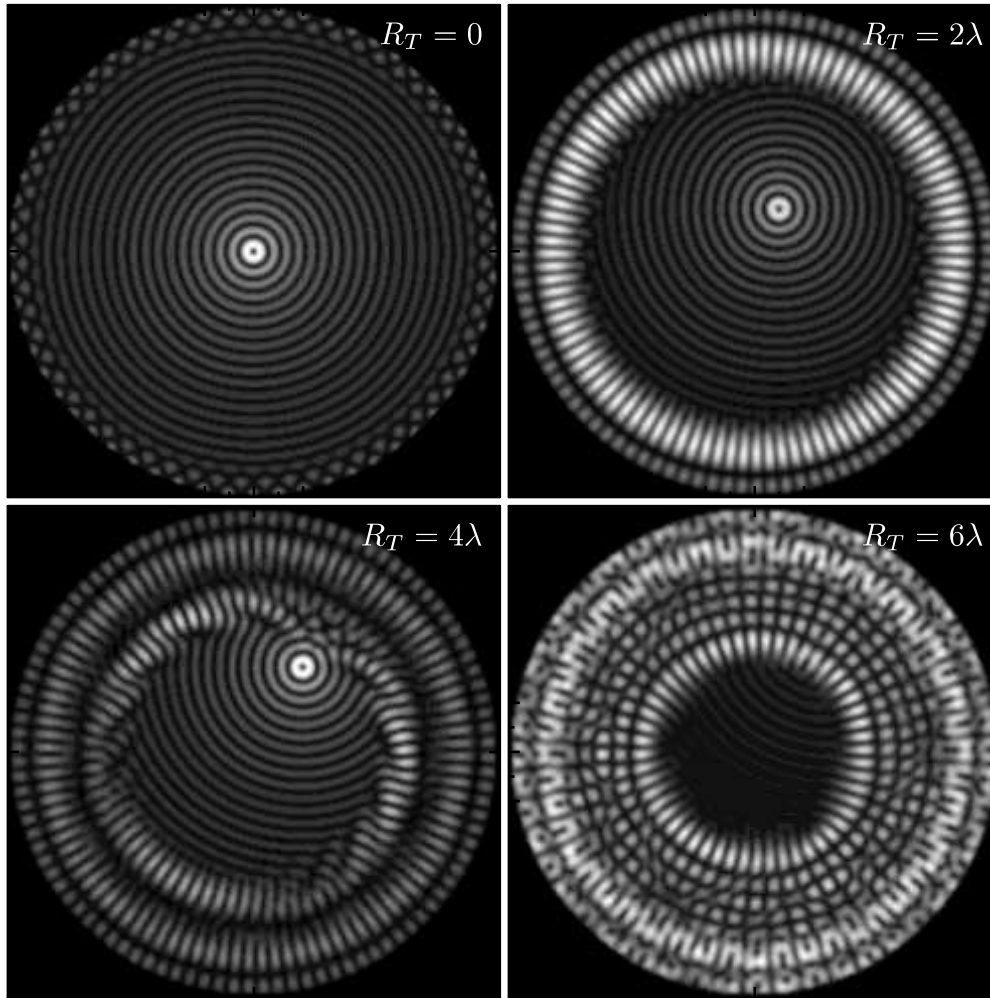


# 🔥 Effect of the number of elements



# Performance limits and aliasing

N=60



- If the boundary is discretized, then, according to sampling theorem an inevitable aliasing appears

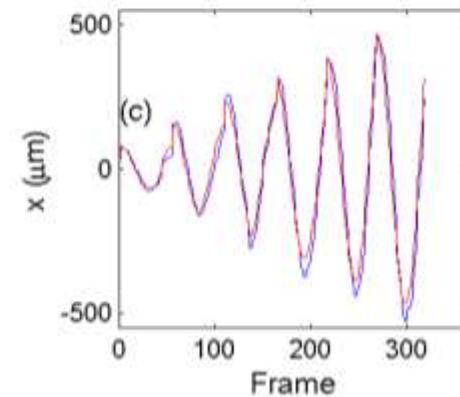
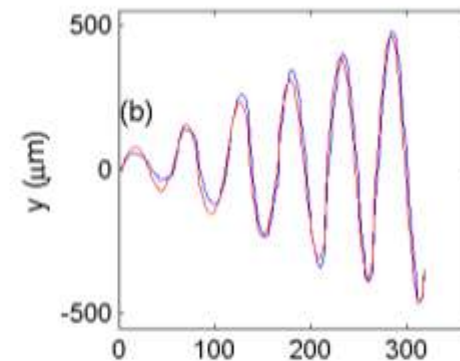
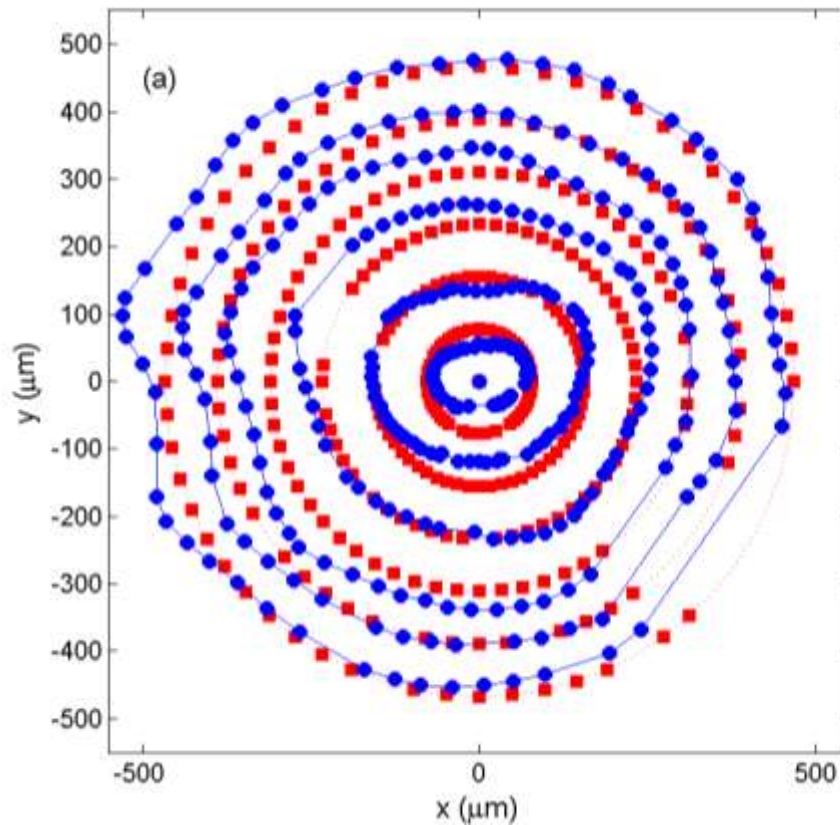
$$p(\mathbf{r}) = \underbrace{p_0 J_\alpha(kR_T) e^{i\alpha\theta_T}}_{\text{Target field}} + \underbrace{p'(\mathbf{r})}_{\text{Artefact field}}$$

- Controllable area is defined by:

$$R_{T(Max)} = \frac{1}{2} \frac{(N - \alpha)}{\pi e} \lambda$$

$$\approx \frac{N\lambda}{17.08}$$

# Particle positioning





# Multiple traps

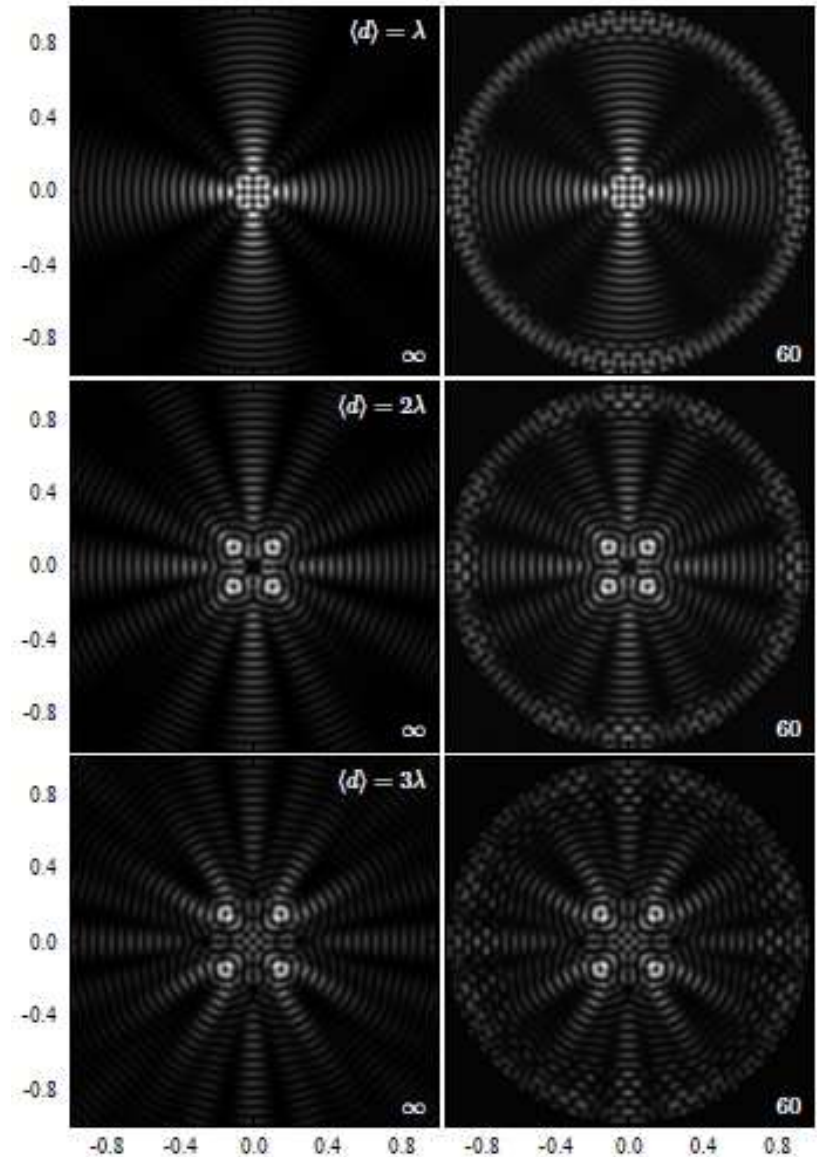
- $n^{\text{th}}$  element and  $m^{\text{th}}$  trap

$$\phi_{nm} = \left( \frac{2\pi(n-1)}{N} - kr_{nm} \right)$$

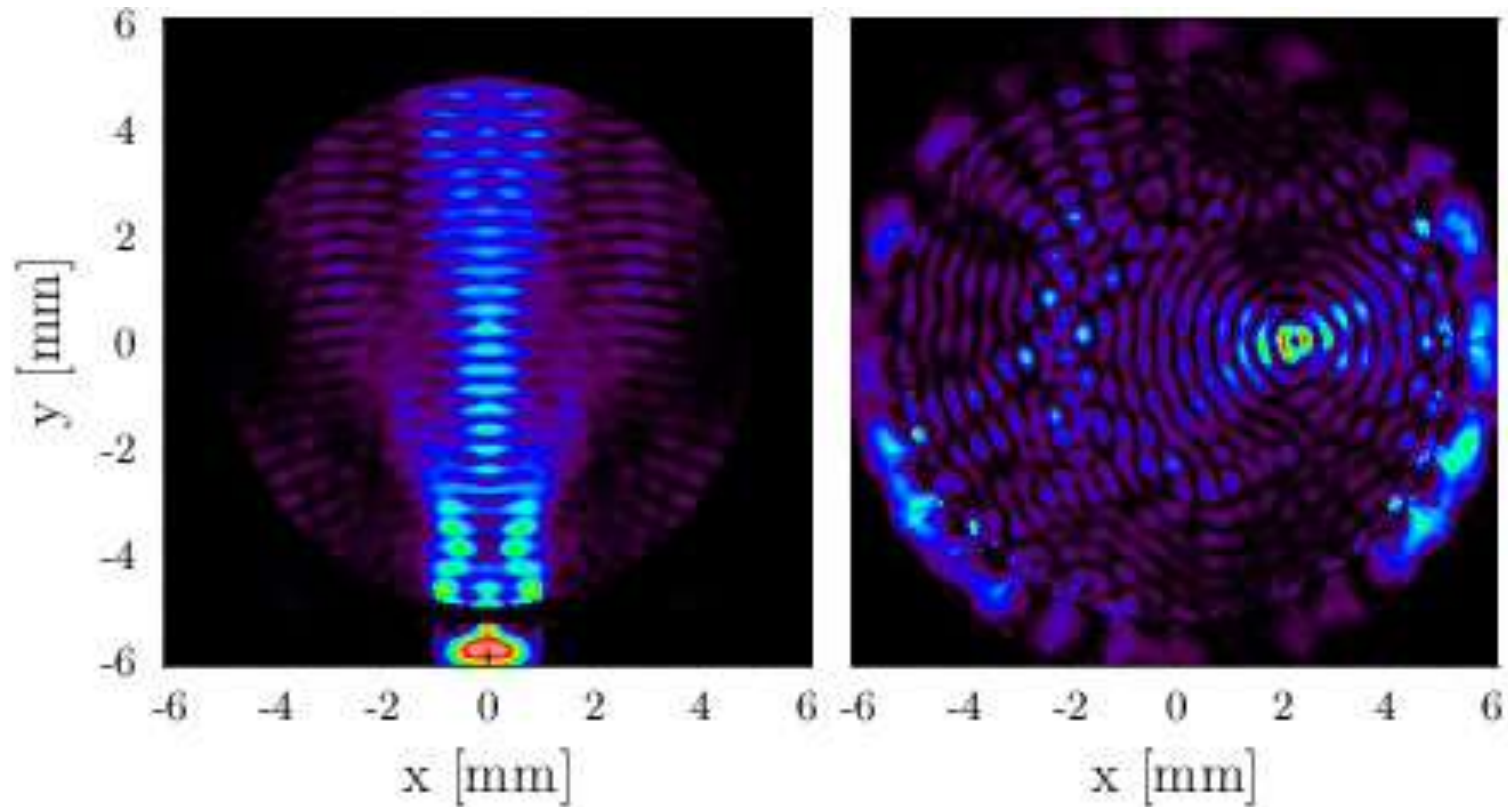
$$V_{nm} = V_0 \exp(i(\omega t + \phi_{nm}))$$

- Linear superposition.

$$V_n = \sum_{m=1}^M V_{nm} = V_n' \exp(i\phi_n')$$



# 🔥 Full FE simulation of 32-element array device

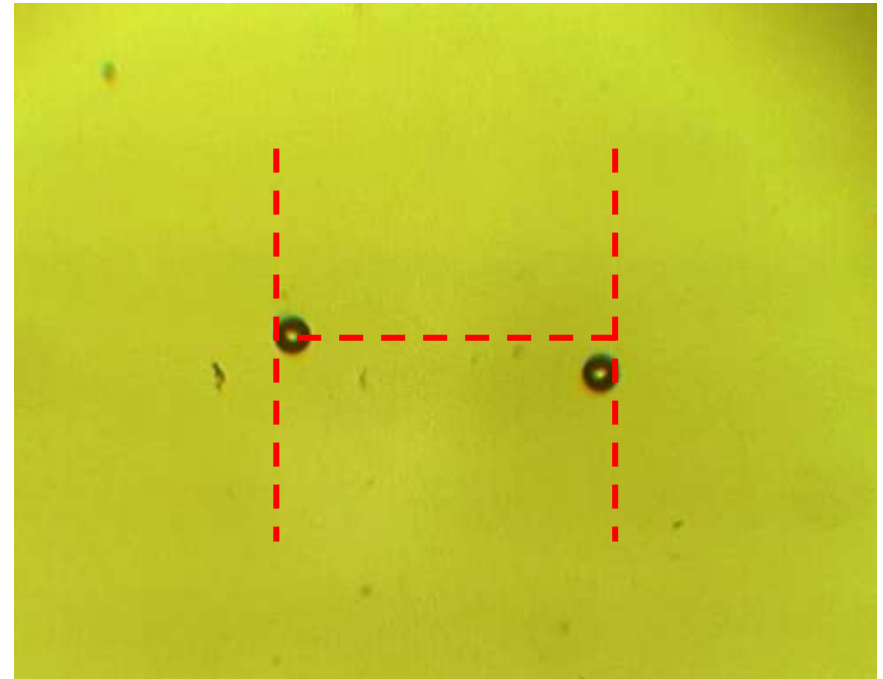


# 🔥 2 traps moving and merging

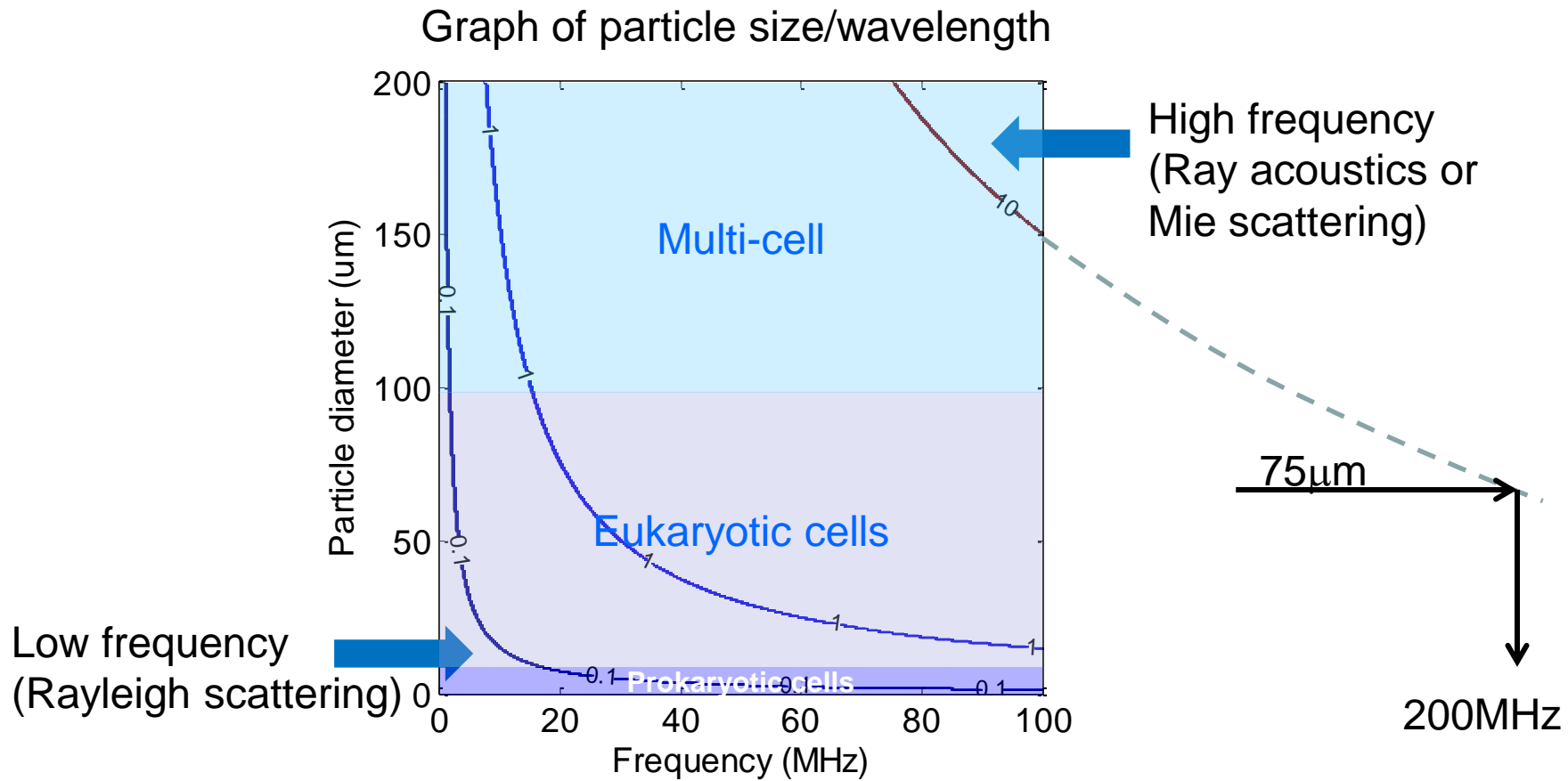
Schlieren



Video

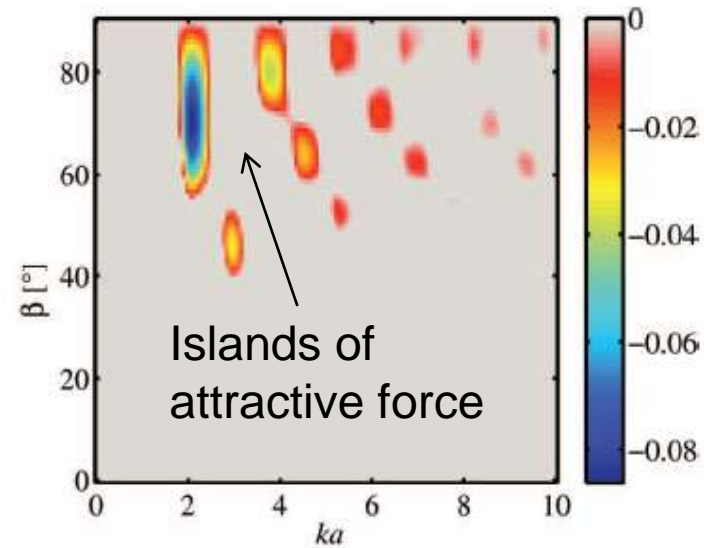
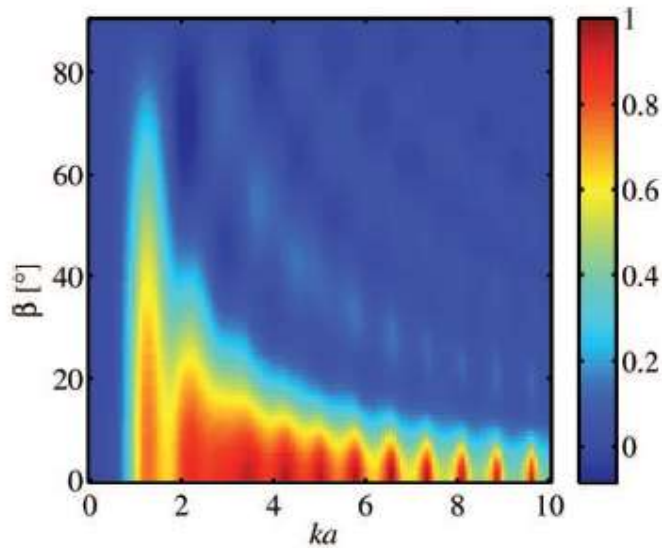
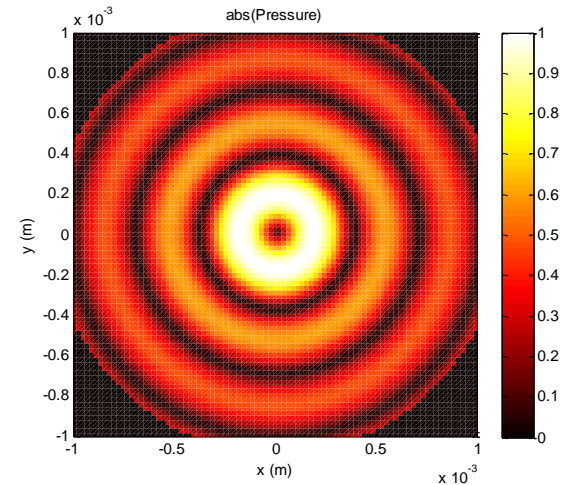


# 🌟 What does high and low frequency mean in practice?

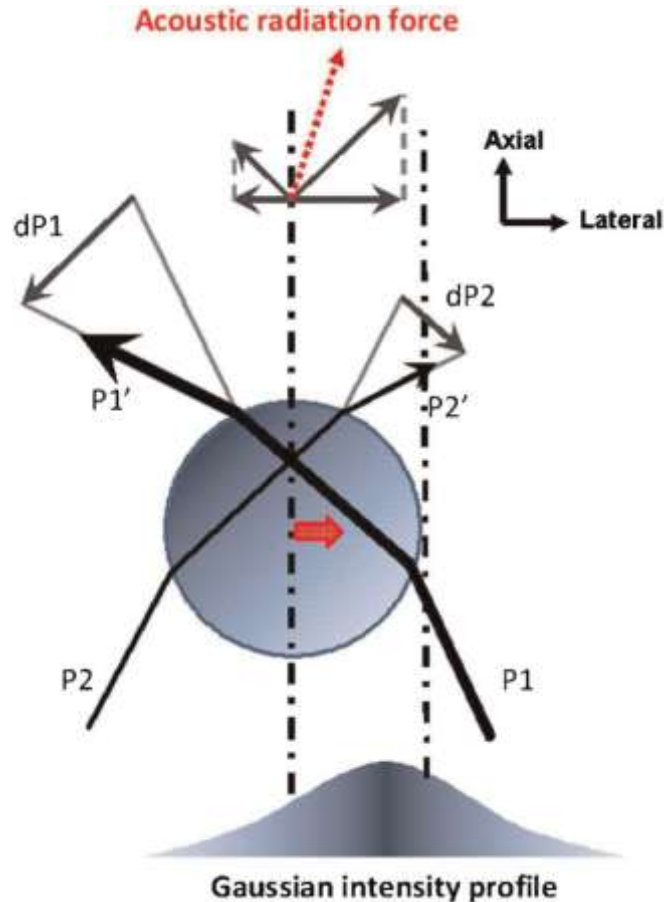


# 🔥 Propagating Bessel beams

$$p = e^{ikz \cos \beta} J_{\alpha}(k\rho \sin \beta) e^{i\alpha\varphi}$$



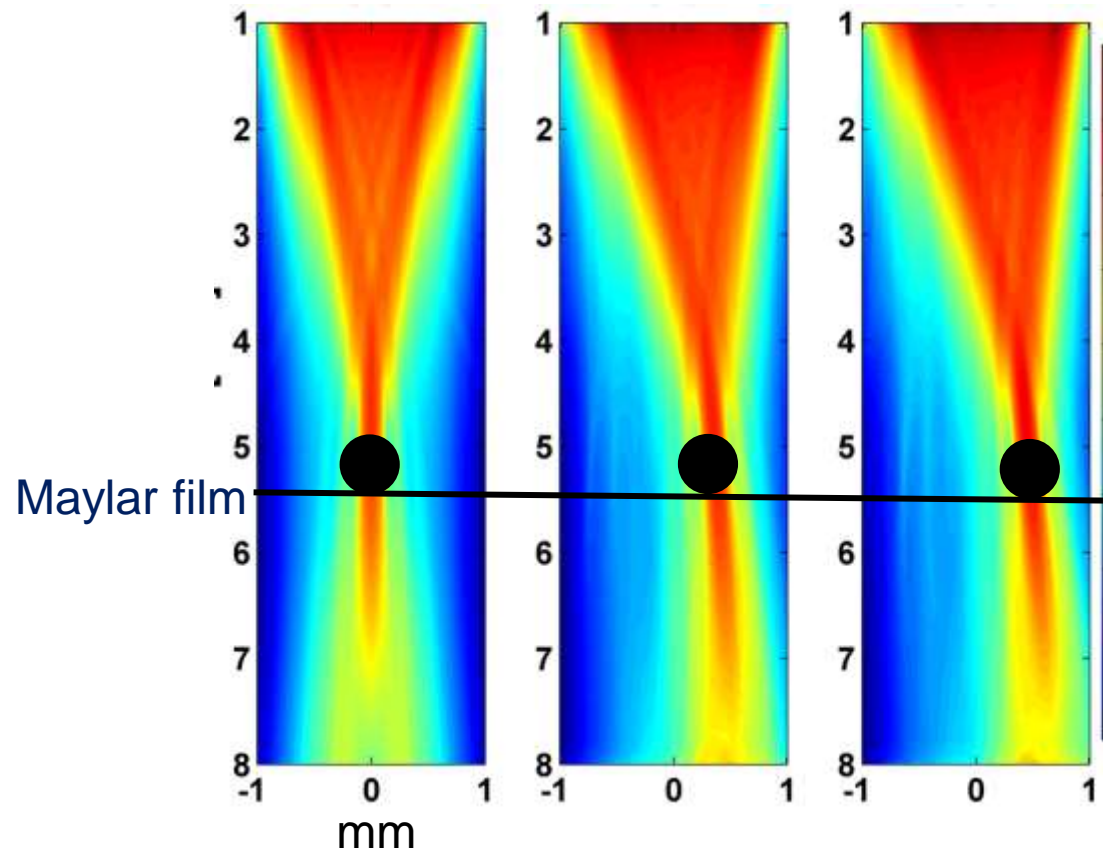
# 🔥 High frequency force regime



- $a \gg \lambda$  (ray acoustics)
- In 2010 Lee et al trapped a  $125\mu\text{m}$  lipid drop using 30MHz ultrasound ( $\lambda=60\mu\text{m}$ )
- In 2011 Lee et al<sup>+</sup> trapped a Leukaemia cell ( $10\mu\text{m}$ ) using 200MHz ultrasound ( $\lambda=7.5\mu\text{m}$ )

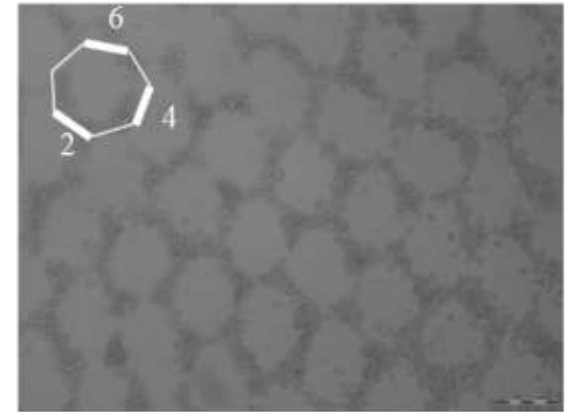
# High frequency array

- 26MHz  
( $\lambda=58\mu\text{m}$ ), 64  
element array\*
- $\text{\O} 45\mu\text{m}$  PS
- Standard phased  
array focussing

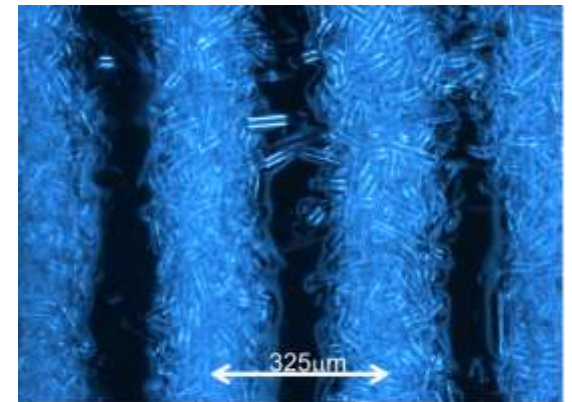


# Applications

- Biology (e.g. tissue engineering)
  - High precision, high dexterity
  - Scale fixed by cell/tissue size
  - Non-destructive to cells
- Medicine (e.g. drug delivery)
  - Moderate precision, moderate dexterity
  - Scale fixed by delivery agent
  - Single sided
  - Destructive?
- Materials (e.g. composites)
  - Moderate precision, moderate dexterity
  - Large area, multi-scale
  - Fast
  - Flexible in terms of materials
  - No living matter involved



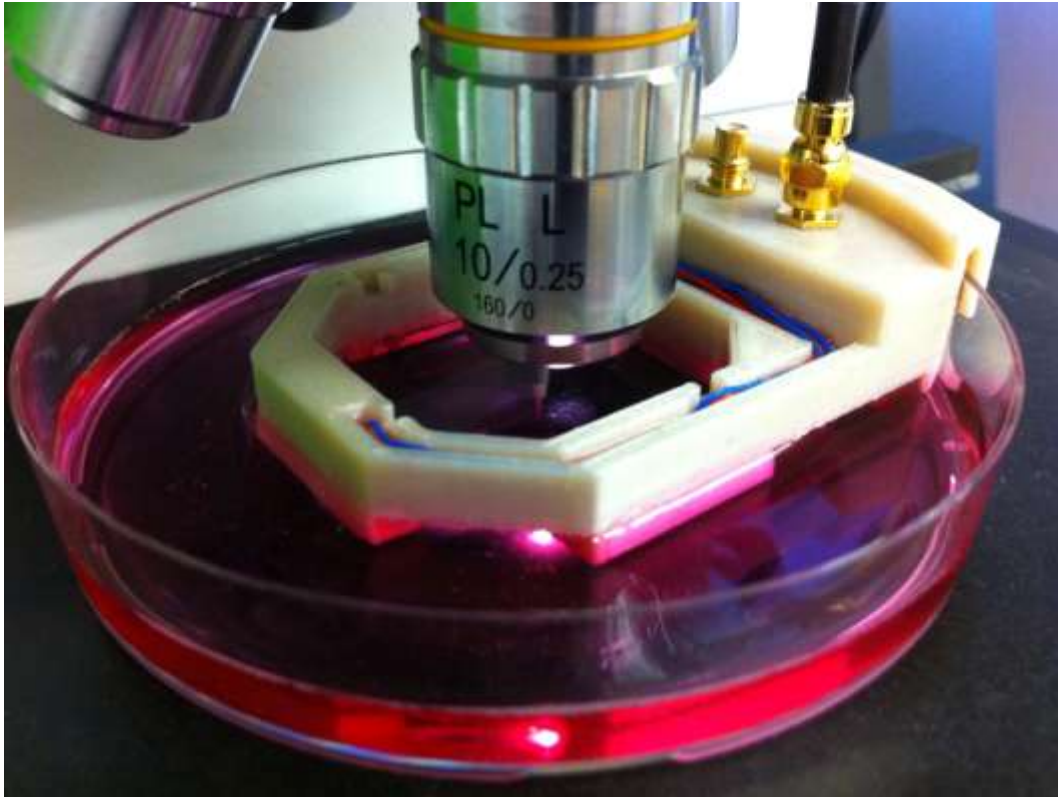
MDCK Cells (Photo courtesy of Anne Bernassau, University of Glasgow)



Glass fibres set in epoxy resin (Photo courtesy of Marc Scholz, University of Bristol)

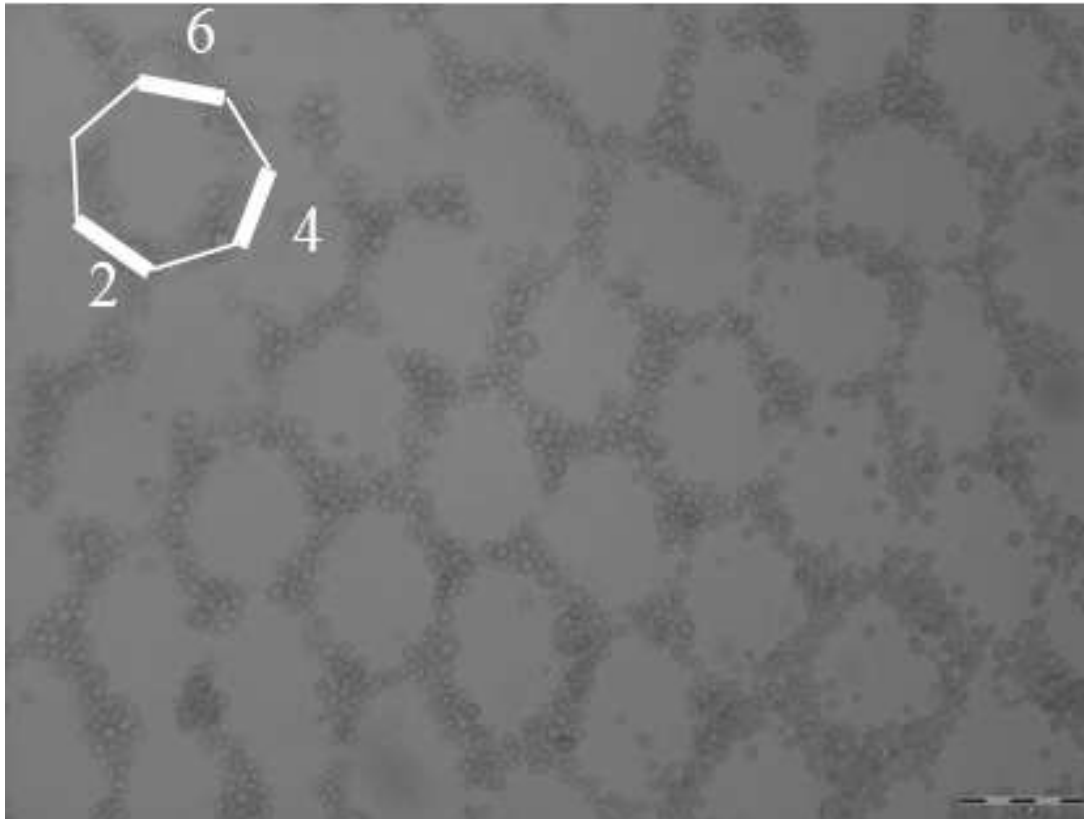


# 🌿 Cell patterning



- Biocompatible acoustic manipulator printed with rapid prototyping system
- Fits within a petri dish
- 15x15mm active area
- Easy to sterilise
- Good optical access

# 🔥 Cell patterning



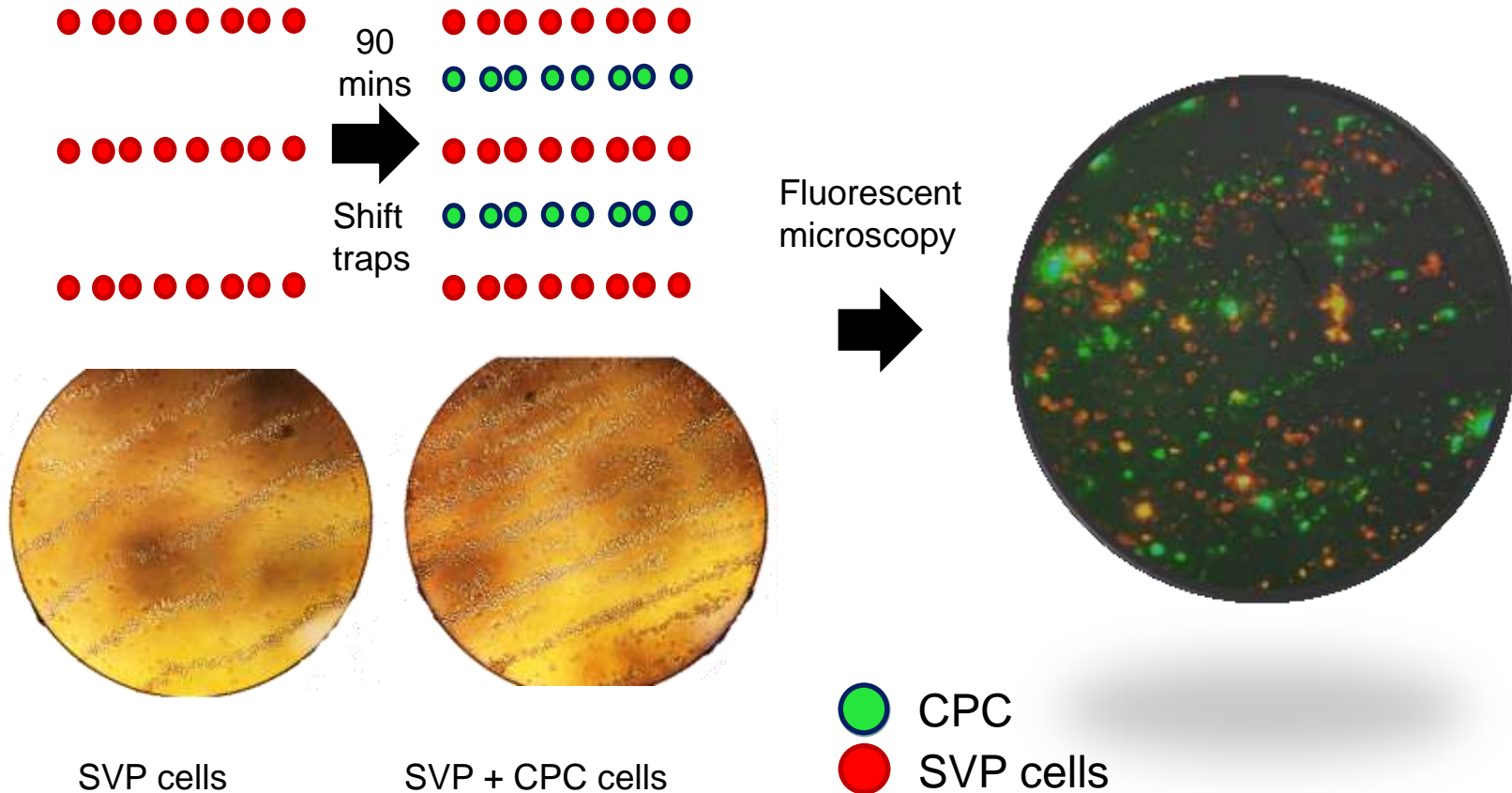
## Uses include;

- Cell-cell and cell-chemical interaction studies
- Forming the building blocks of engineered tissue
- Various new migration and/or adherence assays

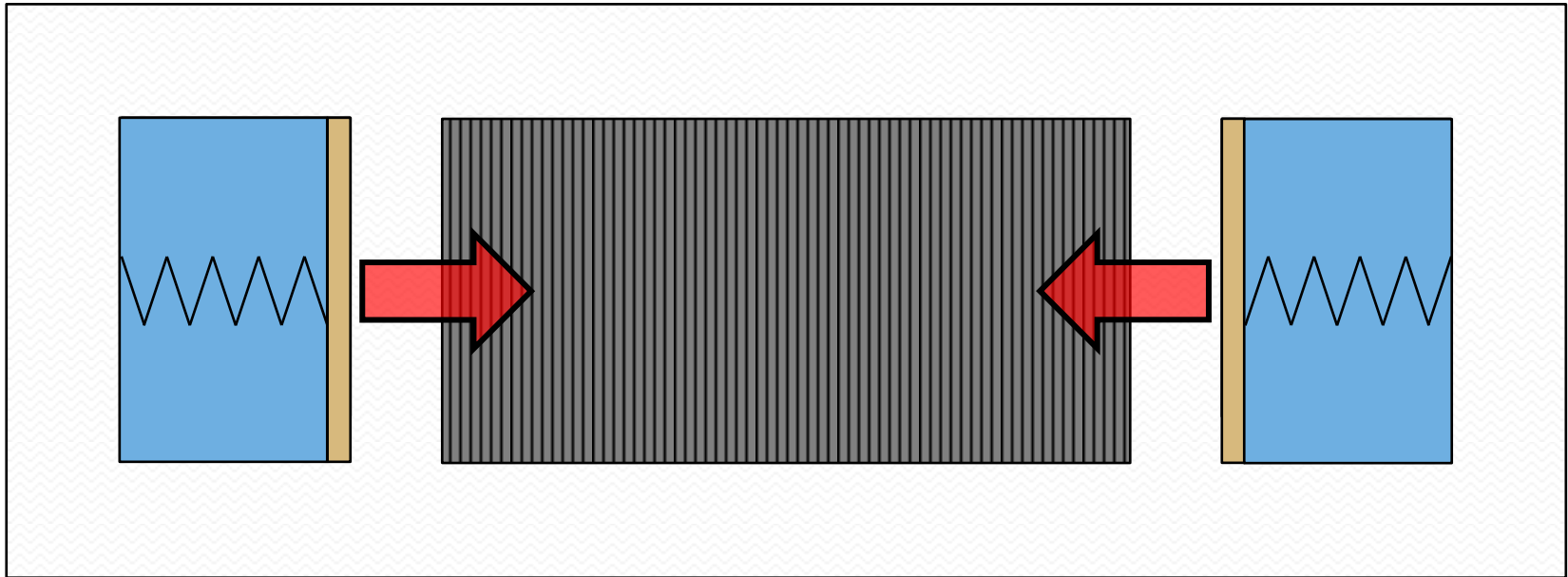
MDCK Cells (Photo courtesy of Anne Bernassau, University of Glasgow)



# 🌿 Co-culturing cells



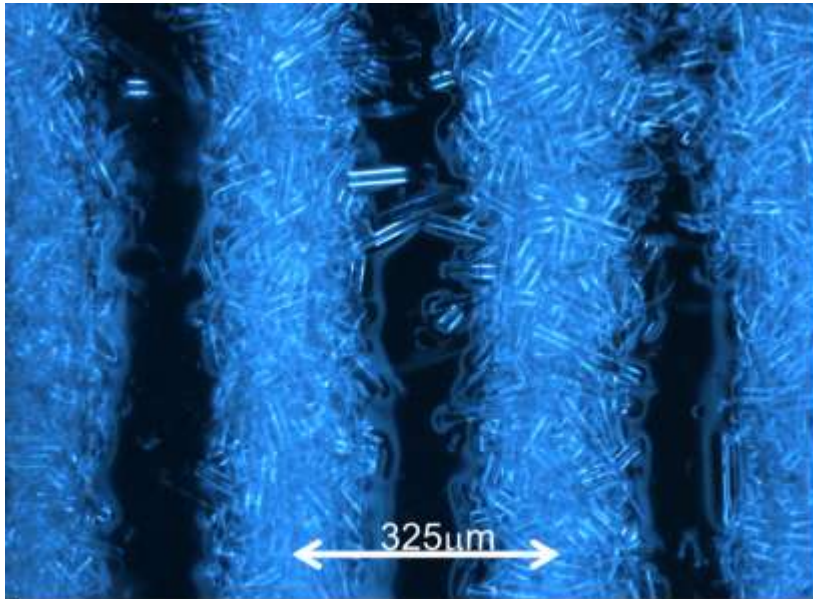
# Composite manufacture



- Low viscosity photo-cure epoxy resin
- 15 $\mu\text{m}$  diameter, 50  $\mu\text{m}$  length glass fibres
- Operated at 2MHz, so line spacing equals 325 $\mu\text{m}$

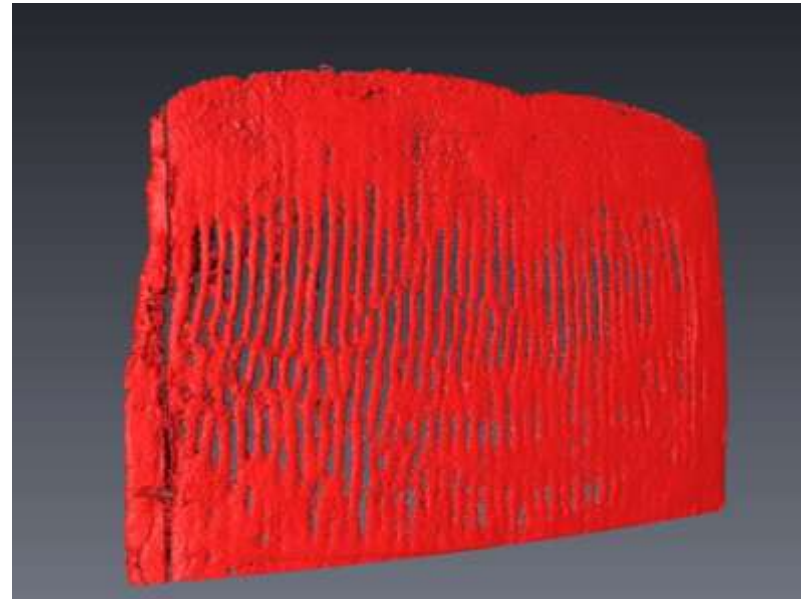
# 🌿 Composite manufacture

Photo



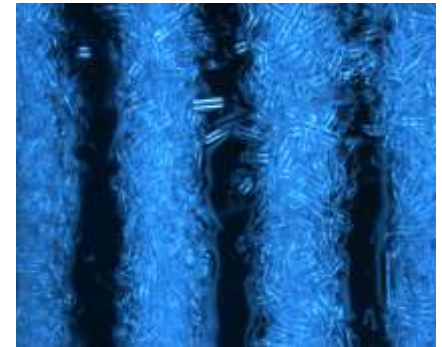
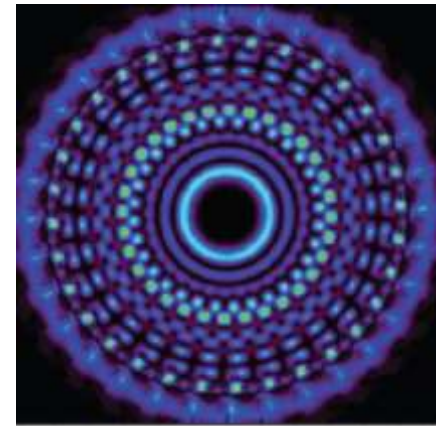
Glass fibres set in epoxy resin (Photo courtesy of Marc Scholz, University of Bristol)

X-ray CT



# ✦ Concluding remarks

- Dexterous acoustic tweezing is a reality
- Various concepts are being explored and showing significant promise
- Typically devices use wavelengths  $\sim 100\mu\text{m}$  to manipulate cells  $\sim 10\mu\text{m}$  in water (i.e. complimentary to optical tweezers)
- Order of magnitude variation in these length scales is possible
- Applications includes tissue engineering and micro/nano fabrication





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# **How to make an acoustic tweezer**

Professor Sandy Cochran  
University of Dundee, UK

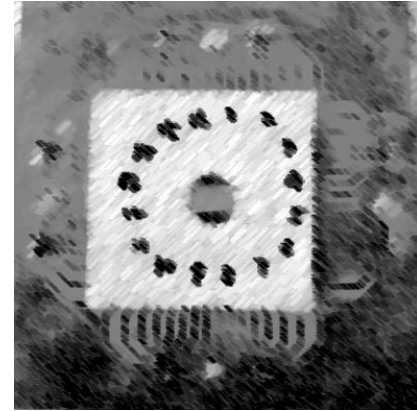
IEEE International Ultrasonics Symposium  
Prague, Czech Republic  
21 July 2013

# Course Outline

- This part of the course focuses on Sonotweezers as **arrays of individual devices**
  - Acoustic tweezing and sonotweezing may also refer to simpler devices
- The components of a **Sonotweezer**
  - The tweezer itself
    - Piezoelectric material
      - Micromachining
    - Other components
  - The **electronics**
    - Conventional multichannel excitation
    - Array controllers
    - Maximally simplified electronics
  - **Ancillary components**

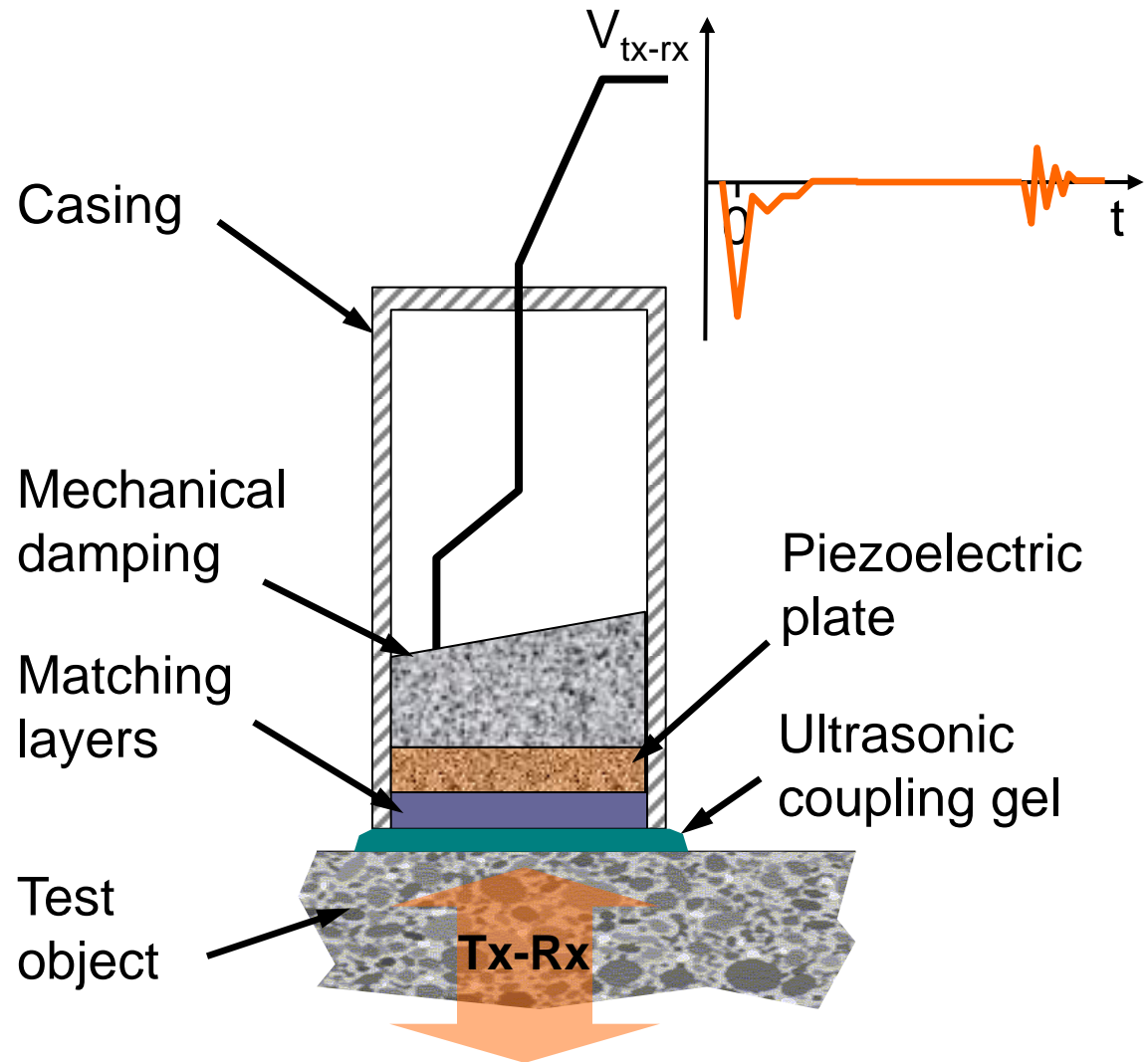


# The Components of a Sonotweezer



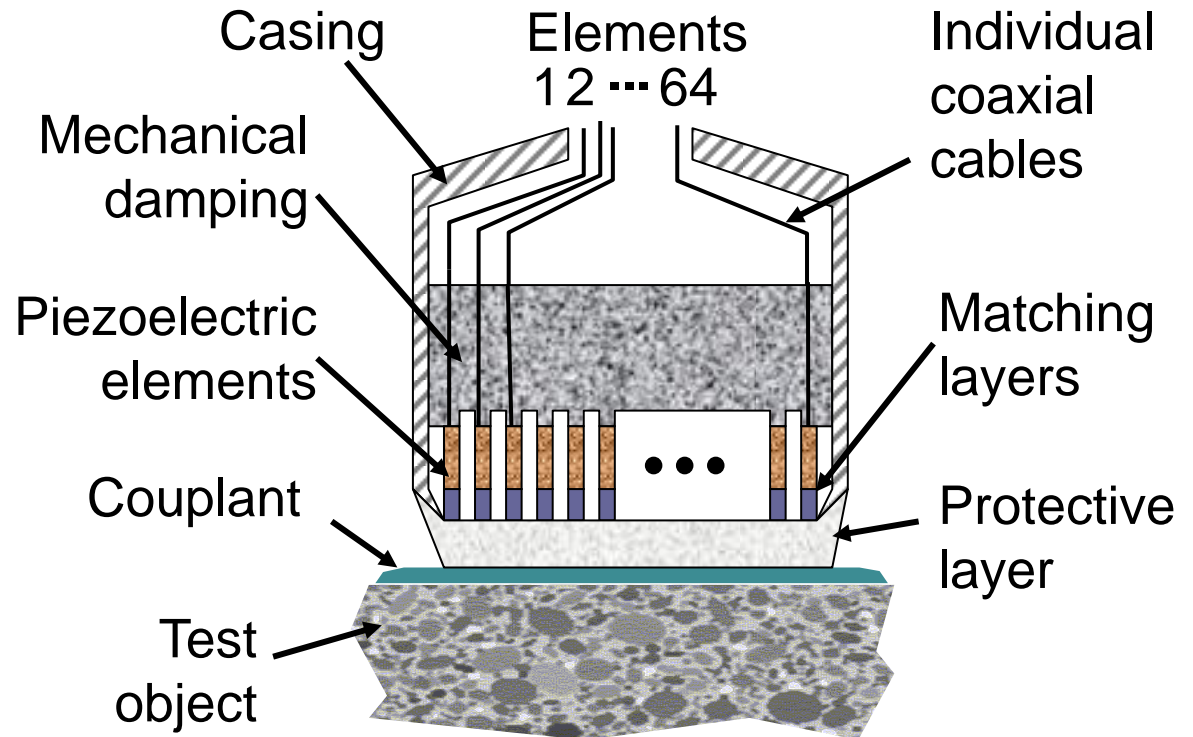
# Conventional Transducer Structure

- Classic **single element** transducer



# Ultrasonic Array Structure

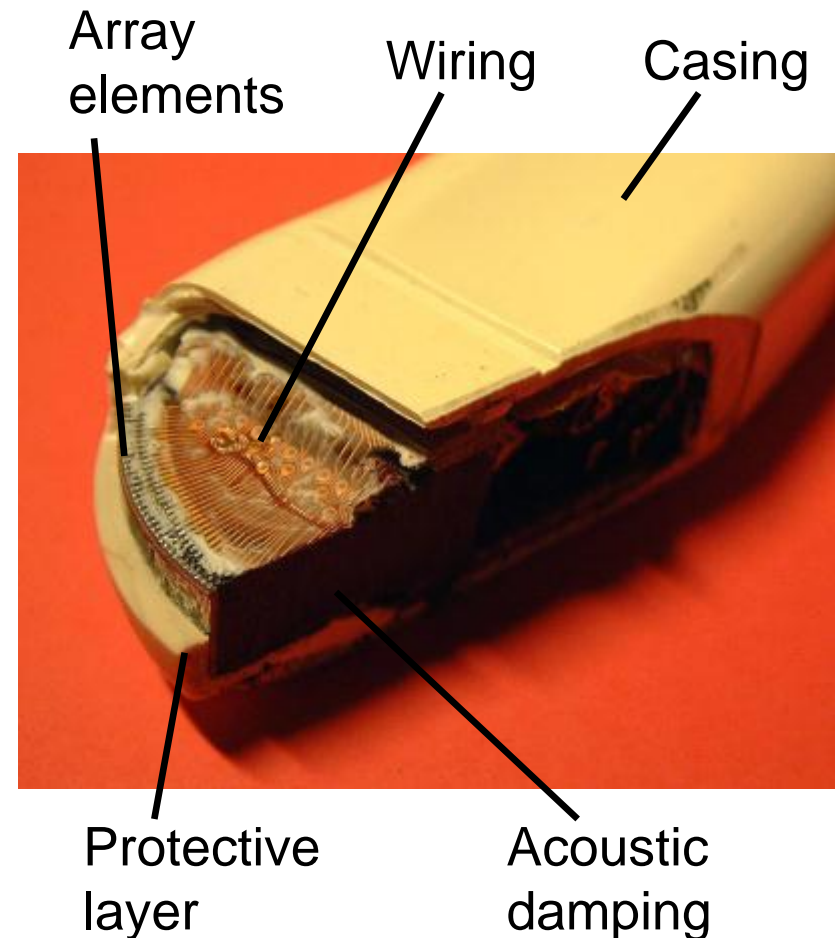
- An array is a **set of miniature transducers** known as array elements
- The array elements are in **fixed, known positions** relative to one another



# Medical Implementation

- Arrays are implemented with an **integrated manufacturing process**

- The array is first made with all the elements joined together, using monolithic pieces of the active material and other layers
  - The elements are **separated in situ**
- This approach is also ultimately the **only practical one** for Sonotweezers

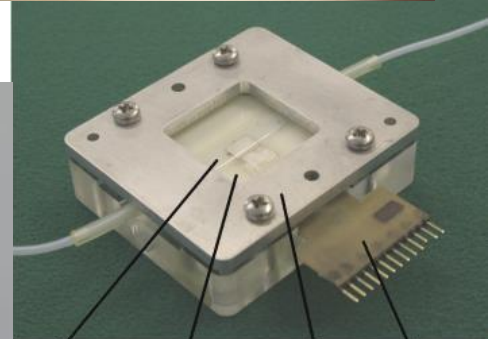
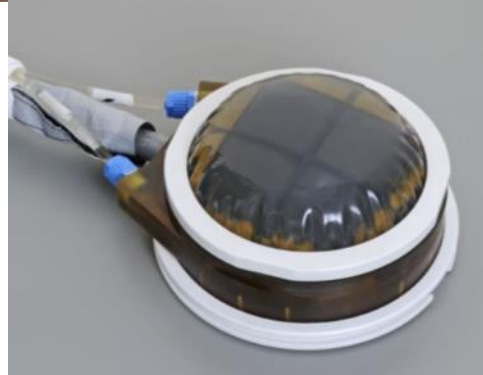
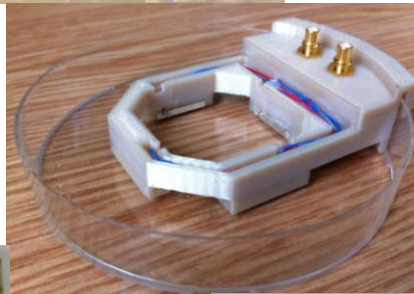
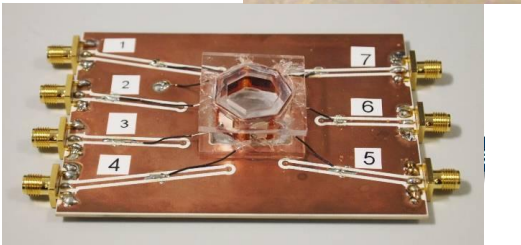
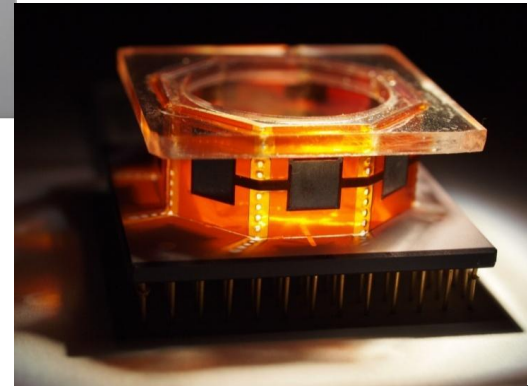
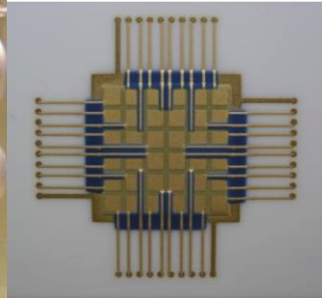
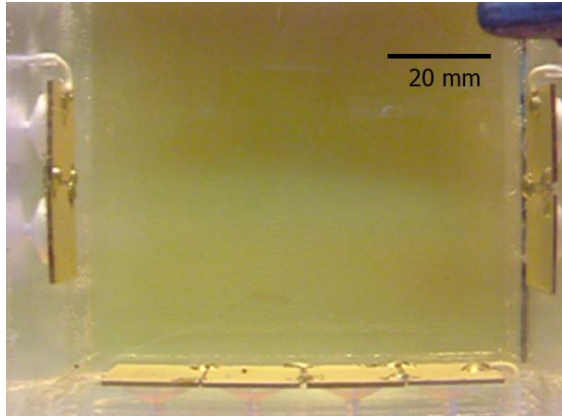


# Sonotweezer Arrays

- **Piezoelectric elements**
  - Still required as a set of miniature transducers
    - Individual electrical connections also a necessity
- **Mechanical damping**
  - Acoustic tweezers are narrowband ultrasound sources
    - Hence mechanical damping is not needed
- **Matching layers**
  - Needed for some acoustic tweezers but not all
    - Can be omitted for simple, exploratory devices
- **Casing etc**
  - Designed ad hoc according to application
  - Unlikely to require protective front face layer

# Examples

Not to scale



Glass capillary  
Transducer plate (front face)  
Housing  
PCB and connectors

# Related Design Framework

Dimensionality	3D	3D array manipulator with mode switching				Insightec Matrix Array	
	2.5D	Crossed electrode array manipulator	2D array manipulator	Dual pair matched transducers	64-element device		
	2D	2D multi wave- $\lambda$ resonator			SAW counter propagating device		
				Heptagon-on-flex device	Octagon-on-flex device		
	1.5D	Linear array manipulator		Single pair matched transducers			
	1D		Mode switched $\frac{1}{2} \lambda$ resonator				
			Ring transducers				
		HF SAW multi- $\lambda$ capillary resonator	HF multi- $\lambda$ capillary resonator				
		Multi- $\lambda$ vertical resonator	HF multi- $\lambda$ lateral resonator				
			Acoustic Cytometer				
		Transwell chamber	SAW microchannel lateral resonator				
	0.5D	Bead sorter	LNO $\frac{1}{2} \lambda$ resonator with capillary				
		Thin layer resonator	$\frac{1}{2} \lambda$ resonator with capillary				
$\frac{1}{2} \lambda$ resonator		$\frac{1}{4} \lambda$ resonator					
	Resonant Chamber Devices		Counterpropagating Wave Devices		Progressive Wave Devices		

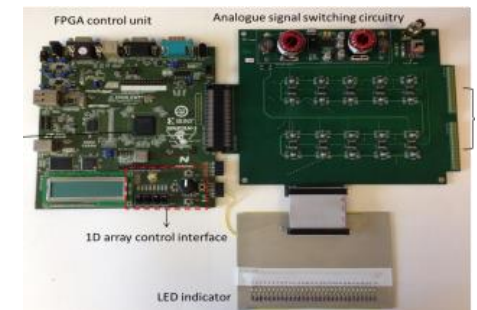
# Related Design Framework

Dimensionality	3D	3D array manipulator with mode switching		[Blue Box]		Insightec Matrix Array	
	2.5D	Crossed electrode array manipulator	2D array manipulator	Dual pair matched transducers	64-element device	[Red Box]	
		2D multi wave- $\lambda$ resonator		SAW counter propagating device			
	2D			[Yellow Box]		Heptagon-on-flex device	Octagon-on-flex device
		1.5D	Linear array manipulator		Single pair matched transducers		[Light Pink Box]
	1D	[Red Box]		Mode switched $\frac{1}{2} \lambda$ resonator	[Large Red Box]		[Large Red Box]
		[Red Box]		Ring transducers			
		HF SAW multi- $\lambda$ capillary resonator	HF multi- $\lambda$ capillary resonator				
		Multi- $\lambda$ vertical resonator	HF multi- $\lambda$ lateral resonator				
		Acoustic Cytometer					
0.5D	Transwell chamber	SAW microchannel lateral resonator	[Large Red Box]		[Large Red Box]		
	Bead sorter	LNO $\frac{1}{2} \lambda$ resonator with capillary					
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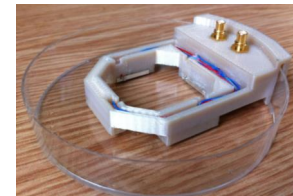
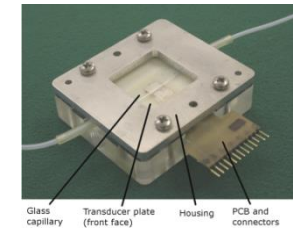
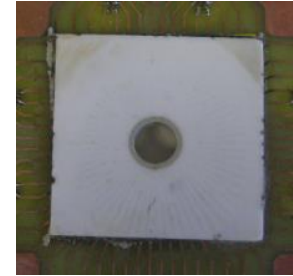
# Electronics

- Three choices
  1. Based on commercial **multichannel signal generators**
    - May need additional output amplification
  2. A commercial ultrasound **array controller**
    - Typically supplied for nondestructive testing
      - May not have sufficient drive capability
    - Alternative is system for focused ultrasound surgery
      - Likely to be low frequency / high power
  3. Fully **custom electronics**
    - Field programmable gate array (FPGA) control likely to be essential
      - With additional simple analogue electronics

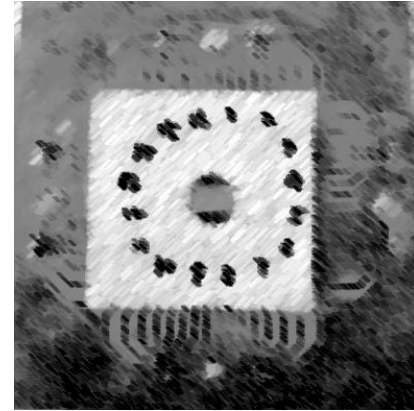


# Ancillary Components

- Some Sonotweezers may contain the working fluid and cells within their structure
  - These devices will either have to be experimental or disposable
- As an alternative, detachable components can be used to contain the working fluid
  - A very wide range of **glass capillaries** is readily available
    - These are inexpensive, mass produced items suitable as **disposables**
    - Their **dimensions can vary significantly** relative to acoustic requirements
  - A Sonotweezer can be designed to fit in a **petri dish**
  - Other specific plastic or glass components could be manufactured

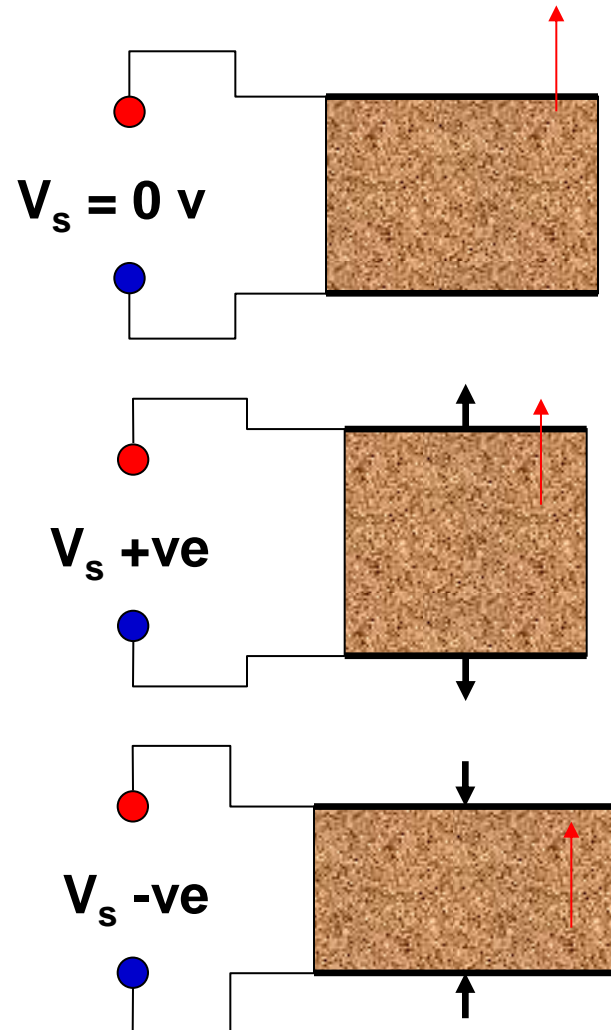


# The Tweezer Itself



# Piezoelectric Material

- Tweezers need **pressure to be generated** in response to an applied voltage
- **Converse** piezoelectric effect:  
  
When a voltage is applied to a piezoelectric material external pressure is generated
- The relevant parameter is  $d$ , the **piezoelectric charge coefficient** (units  $\text{NC}^{-1}$  or  $\text{mV}^{-1}$ )
  - Typical value  
 $d_{33} = 600 \text{ pmV}^{-1}$



# Possible Piezomaterials

			PZT-4	PZT-5H	PVDF	LiNbO <sub>3</sub>	PMN-PT
			“Hard” piezoelectric ceramic	“Soft” piezoelectric ceramic	Piezoelectric polymer	Traditional single crystal	New, high performance single crystal
Stiffness	$c_{33}^D$	GNm <sup>-2</sup>	155	159	8.52	251	135
Density	$\rho$	kgm <sup>-3</sup>	7500	7500	1760	4640	8000
Velocity	$v$	ms <sup>-1</sup>	4560	4600	2200	7360	4040
Acoustic impedance	$Z = \rho v$	MRayl	34.1	34.5	3.92	34.1	32.3
Piezoelectric strain constant	$d_{33}$	pmV <sup>-1</sup>	289	593	25	5.88	1430
Piezoelectric voltage constant	$g_{33}$	VmN <sup>-1</sup>	26	20	230	22	30
Piezoelectric figure of merit	FOM = $d_{33} \cdot g_{33}$	pmN <sup>-1</sup>	7.51	11.9	5.75	0.129	42.8
Thickness mode coupling coefficient	$k_t$		0.508	0.512	0.190	0.162	0.566
Length-extensional coupling coefficient	$k_{33}$		0.691	0.746	0.130	0.162	0.897
Relative permittivity at constant stress	$\epsilon_{33}^T$		1275	3430	8.4	29.8	3950
Relative permittivity at constant strain	$\epsilon_{33}^S$		638	1470	10-12	29.0	818
Mechanical quality factor	Q		High	Medium	Low	Very high	Low

**All values are indicative only**

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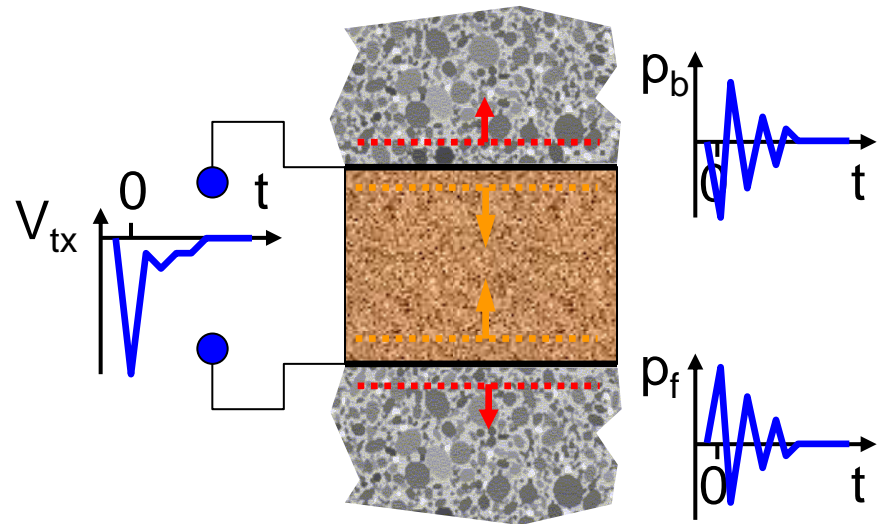
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All values are *indicative only*

# Internal and External Waves

- Excitation voltage,  $V_{HV}$ , is applied, with **desired spectral content**, e.g. sine wave for burst output
- Four distinct mechanical waves are set up
  - Two propagating in the **external media**
  - Two propagating within the **piezoelectric material**
- The waves in the piezoelectric material are **partially internally reflected**, creating an oscillating condition and resonance, with a **frequency inversely proportional to thickness**





# Mechanical Resonance

- **Mechanical resonance** is a fairly straightforward physical effect
  - Hence the frequency,  $f_m$ , is easily determined

$$\lambda = 2D$$

$$f_m = \frac{v}{\lambda}$$

where

$\lambda$  = acoustic wavelength

$D$  = thickness of piezoelectric material

$v$  = acoustic velocity in piezoelectric material

- This **ignores** issues such as piezoelectric stiffening and modification of wave propagation by component shape

# Electrical Resonance

- As the piezoelectric material forms an electrical component (as well as mechanical i.e. it is electromechanical) it also has an **electrical resonance**
  - There is no particularly straightforward way to calculate  $f_e$ , the electrical resonance frequency
  - One way, for wide, thin plates, is to back  $f_e$  out of the expression for **thickness mode coupling coefficient**

$$k_t = \sqrt{\frac{\frac{\pi f_e}{2f_m}}{\tan\left(\frac{\pi f_e}{2f_m}\right)}}$$

- Because the elements in Sonotweezers are **small**, they are likely to **operate best at  $f_e$**

# Matching Layers

- Matching layers are designed to have **anti-reflective** properties to enhance energy transfer from the piezoelectric material through the couplant into the ultrasonic medium
- **Theoretically**, the thickness of a single matching layer,  $T_{ml}$  and its acoustic impedance,  $Z_{ml}$  are defined as

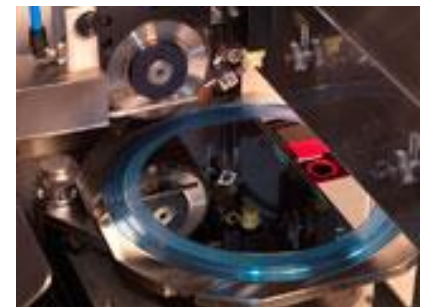
$$T_{ml} = \lambda_{ml} / 4, Z_{ml} = \sqrt{Z_{pm}Z_{um}}$$

where  $\lambda_{ml}$  is the wavelength in the matching layer, and  $Z_{pm}$  and  $Z_{um}$  are the acoustic impedances of the piezoelectric material and the ultrasonic medium respectively

- Although a matching layer works ideally at only a single frequency, corresponding to  $\lambda_{ml}$  it often **increases the operating bandwidth** by reducing reverberation in the piezoelectric material

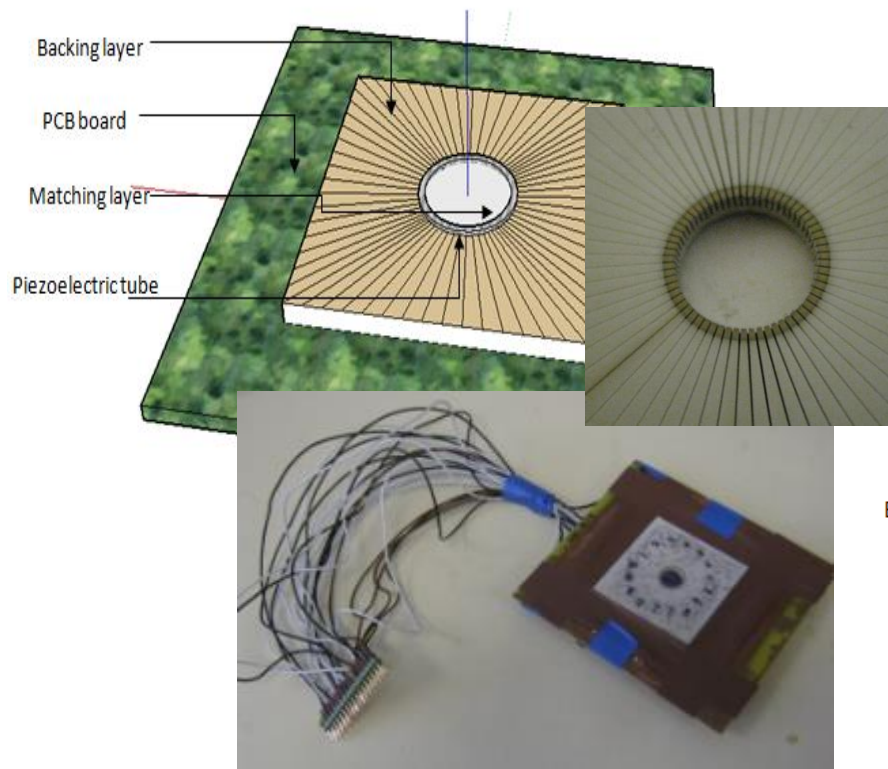
# Micromachining

- Micromachining is needed to generate the **precise shapes** required for the piezoelectric material and the matching layer
- Three possible routes
  - Accessing a **conventional machine shop**
    - Problems with size of tools and machine precision
    - Problems with machining piezoelectric materials
  - Assembling or accessing a **specialised workshop**
    - Key components are dicing saw and lapping / grinding machines
    - Polymer handling / machining also required
  - Utilising **semiconductor / MEMS industry fabrication** processes
    - Highly restricted availability

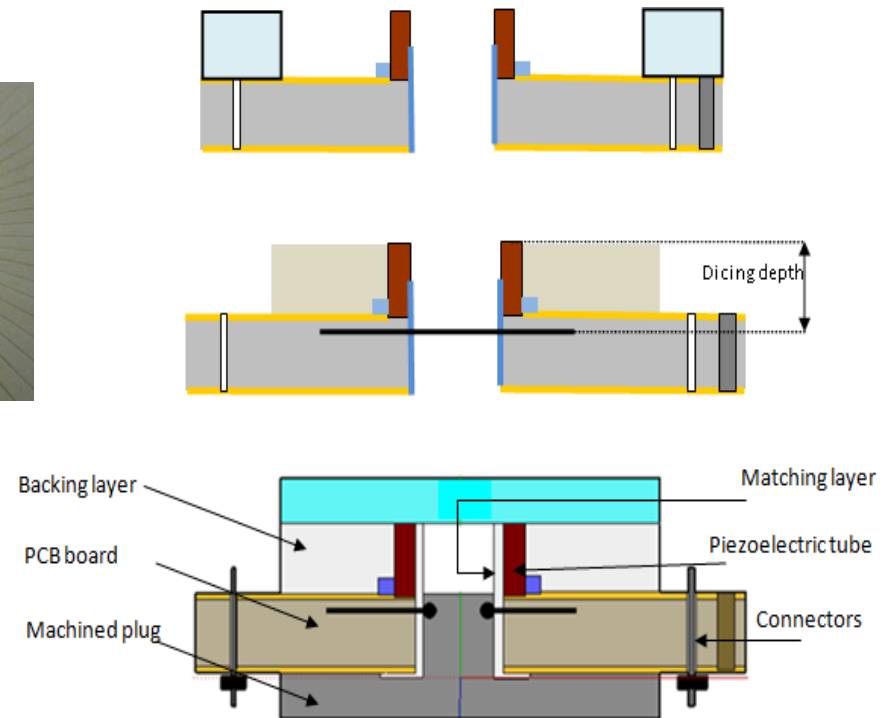


# Example: 64-element Array

## Basic design layout

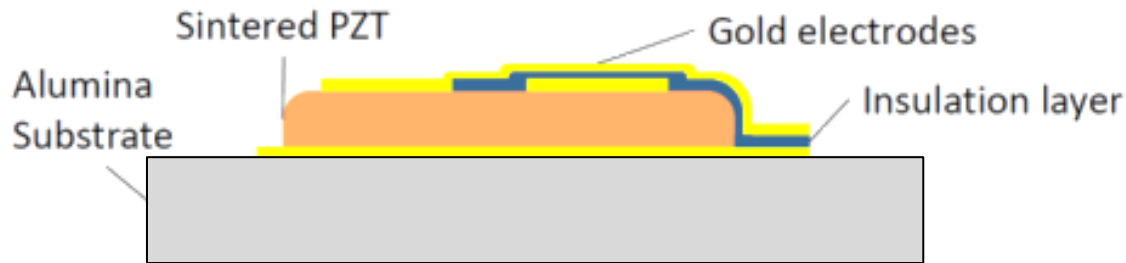


## Fabrication process diagram



- Fabrication process is an **integrated** one
  - Matches **medical ultrasound** approach

# Example: Thick Film Sonotweezer

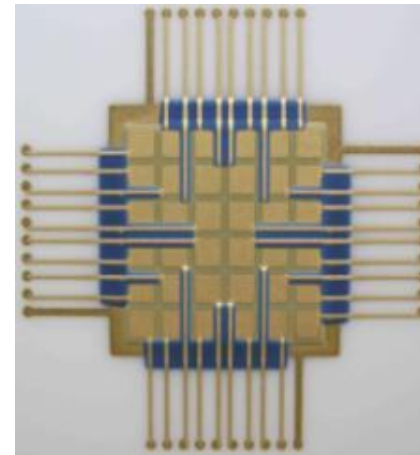


## Electrical interconnect

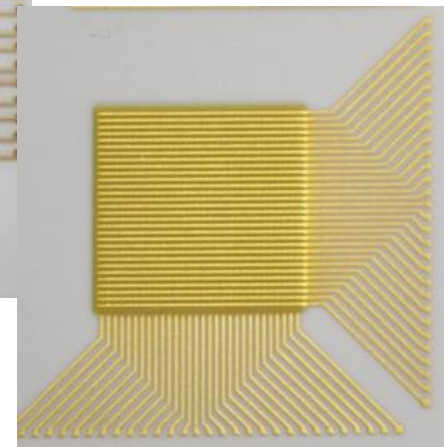
- PZT, Array electrodes and electrode tracks all screen printed on substrate
- Mask-based fabrication

## Fluidic & optical interface

- Array forms base of chamber, or
- Capillary coupled to array

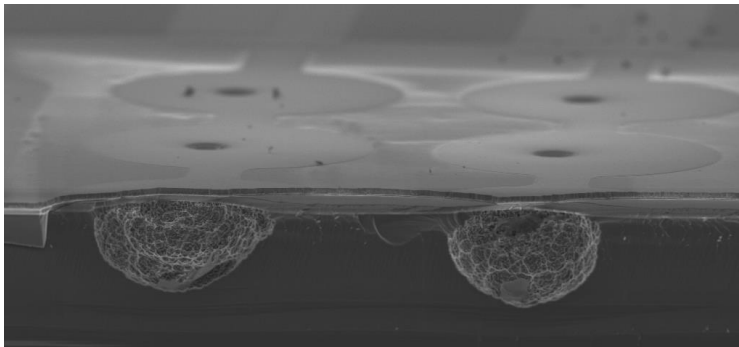
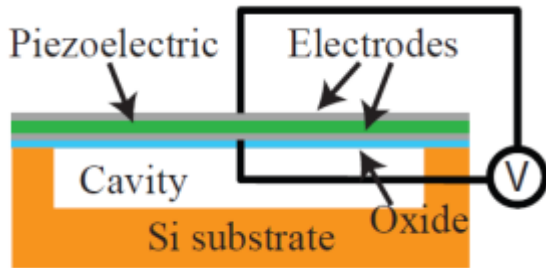


2D Array

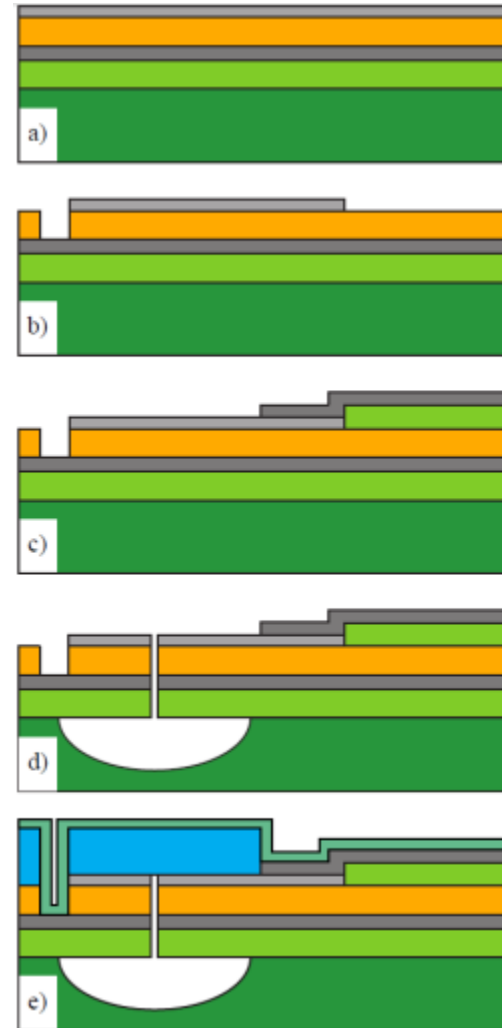


Crossed-  
electrode array

# Example: pMUTs



- Thin film deposition for PZT, array electrodes and electrode fan-out
- Fully mask-based fabrication
- Conventional Si-based microfabrication techniques can be used

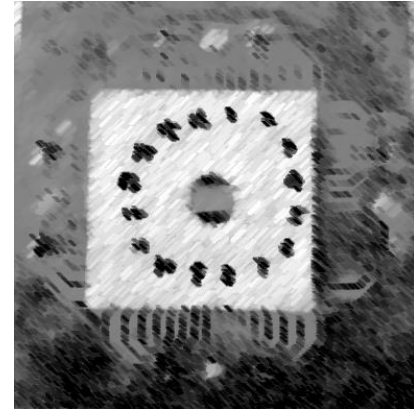


PENNSTATE



Pt  
PZT  
Ti/Pt  
SiO<sub>2</sub>  
Si  
MX5015™  
Parylene-C

# Electronics for Sonotweezers





# Commercial Signal Generators

- Advantages
  - Straightforward solution for **small numbers of elements**
  - Likely to provide **enough drive capability** without additional amplification
  - Offers **easy flexibility**
- Disadvantages
  - **Costly** because of need for flexibility in design
  - Feasible **maximum number of elements limited**
  - **Not** space efficient
  - **Multiple cables** needed: awkward and unreliable



# Commercial Array Controller

- Advantages
  - Should be able to support **enough channels**
  - Provides automatic channel **phasing / synchronisation**
- Disadvantages
  - **May be as costly as separate signal generators**
  - Typically not well matched to Sonotweezers application
    - Will usually include **unnecessary hardware** for reception
    - Will usually **not allow CW** excitation



[www.diagnosticsonar.com](http://www.diagnosticsonar.com)



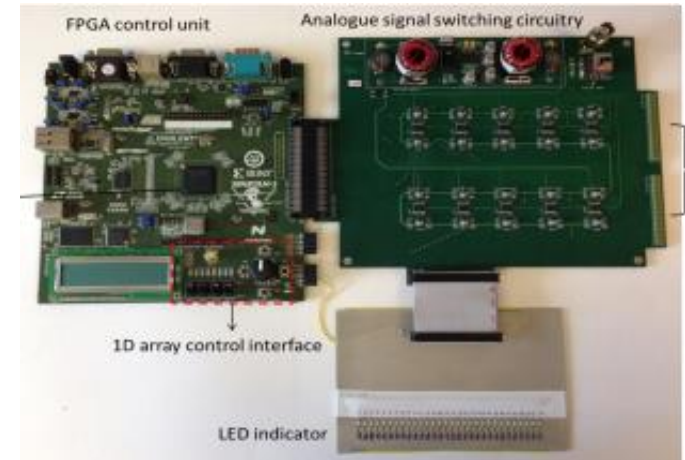
[www.verasonics.com](http://www.verasonics.com)



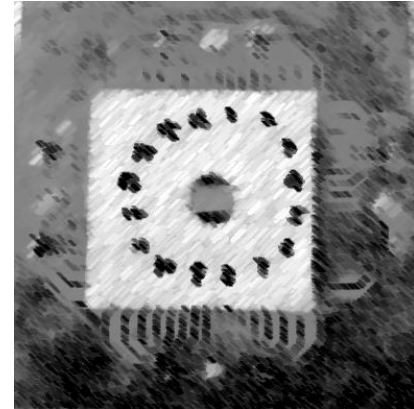
[www.olympus-ims.com](http://www.olympus-ims.com)

# Custom Electronics

- Advantages
  - Relatively **inexpensive hardware**
    - **FPGA** evaluation board
    - Custom analogue drive board
      - Possible to drive Sonotweezers with **rectangular waveforms**
    - **Minimal hardware cost** per channel
    - Automatic **channel phasing** / synchronisation
- Disadvantages
  - **Low level programming** required - VHDL, or LabVIEW option
  - **Custom electronics design** and fabrication required
  - Large channel counts may need **complicated solutions**

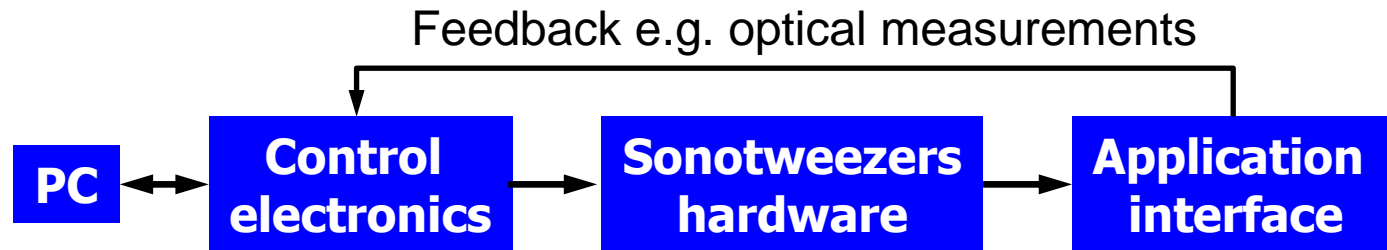


# Ancillary Components



# Ancillary Components

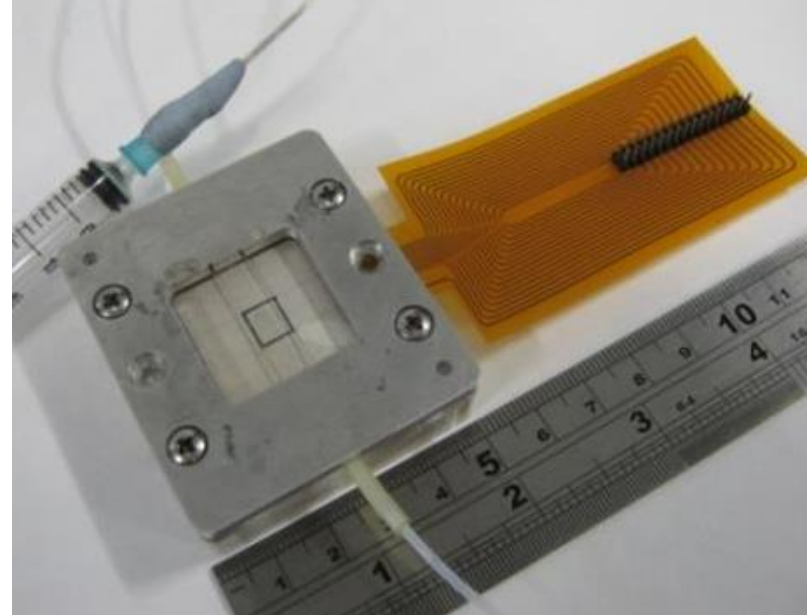
- Translation of Sonotweezers from electronics lab curiosity to useful system requires application-specific front end



- Must work with Sonotweezers
  - Likely also to have to provide additional access for **observation / measurement**
- Must provide access for **target of manipulation**
  - E.g. connection to syringe driver
- Likely to be **disposable** for work in life sciences
  - Capillary, cuvette or petri dish

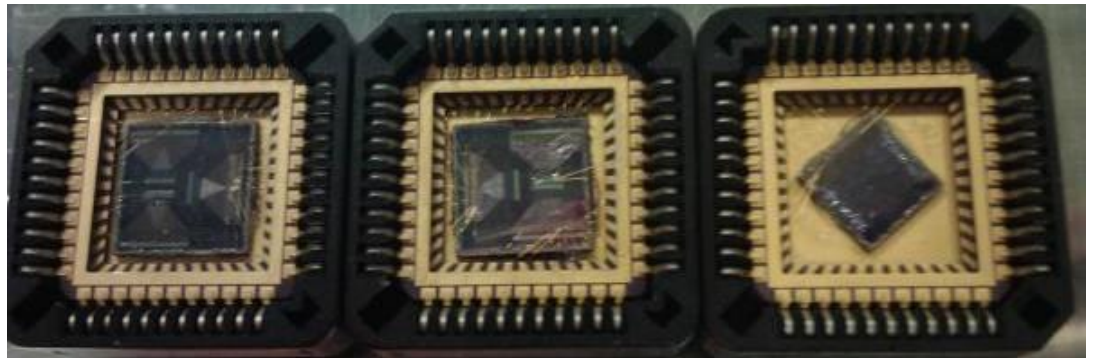
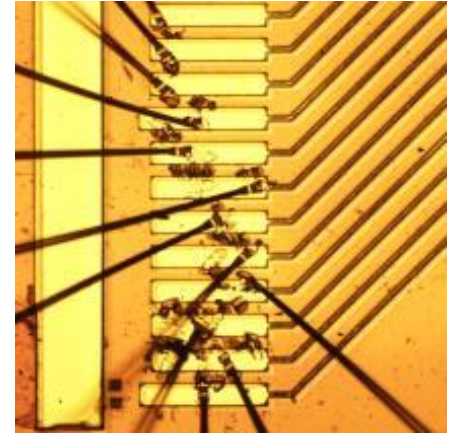
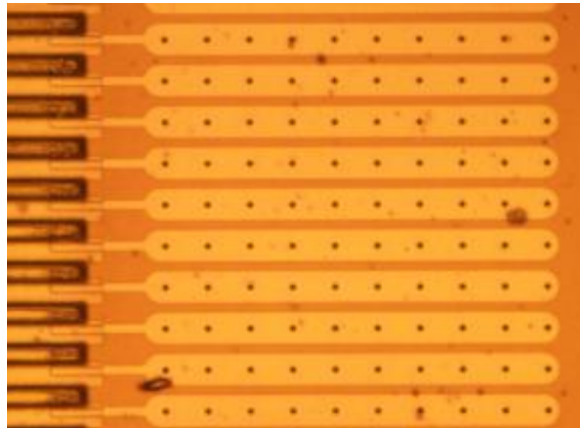
# Example: 1D Array System

- Optical (**observation**) interface
  - Clear glass capillary with open window for microscope observation
- **Fluidic** interface
  - Capillary **coupled** to array substrate
  - Filled / flow controlled from **syringe**

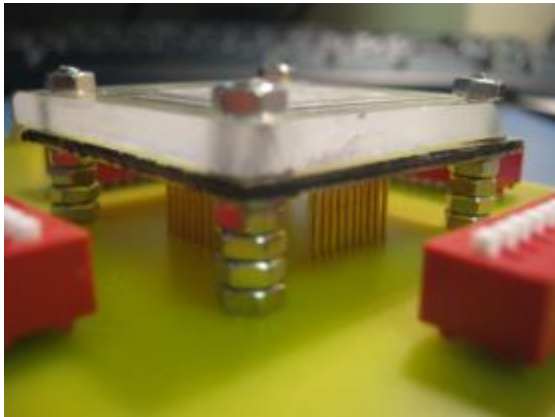
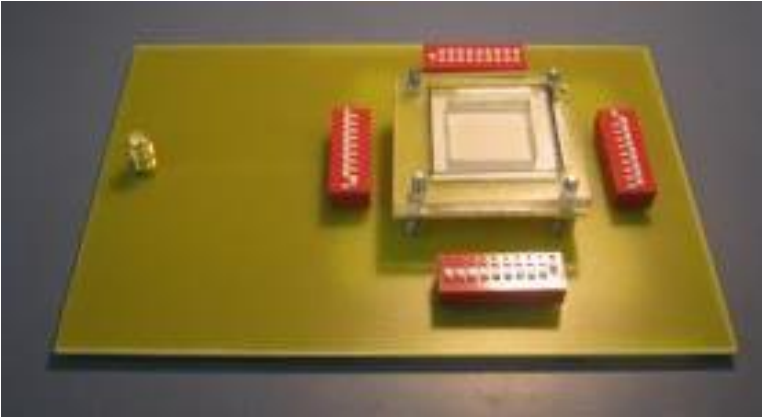
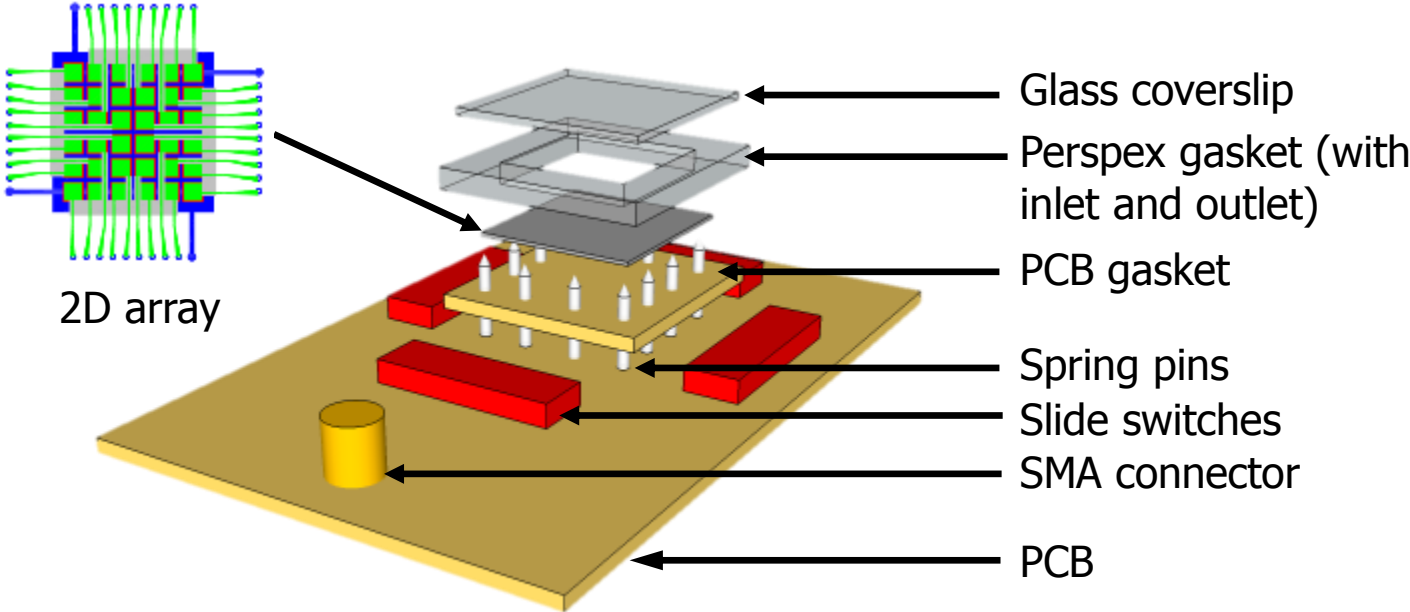


# Example: pMUTs

- Optical (**observation**) from above
- **Fluidic** interface still to be engineered
  - Basis in microscale silicon substrate will require further development
- **Electronic interface** achieved with a chip carrier

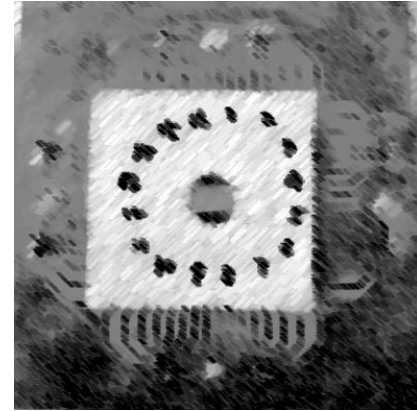


# Example: Thick Film Sonotweezer





# Summary



# Summary

- Sonotweezers development is **bifurcated**
  - **Simple devices** subject to *ad hoc* development
    - **Not** covered here
  - **Multielement devices** requiring specialised fabrication
- Three main components
  - **Sonotweezer** itself
    - Based on micromachined piezoelectrics
  - **Electronics**
  - **Ancillary hardware**
    - Requires **application specific** development
- PC also required for **control** in most systems
- **Many** future possibilities
  - Ultimate target is ultrasound equivalent of **spatial light modulator in optical tweezing**